

LECTURER NOTES

DESIGN OF STEEL STRUCTURES

**B.Tech,6TH Semester,
Civil Engineering**

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COURSE CONTENT

Design of Steel Structure

B.Tech, 6th Semester, CE

Module I

Introduction, advantages/disadvantages of steel, structural steel, rolled steel section, various types of loads, design philosophy. Limit state design method, limit states of strength and serviceability, probabilistic basis for design Riveted, bolted and pinned connections, Welded connections-assumptions, types, design of fillet welds, intermittent fillet weld, plug and slot weld, failure of welded joints, welded joints vs bolted and riveted joints

Module II

Tension members, types, net cross-sectional area, types of failure, slenderness ratio, design of tension members, gusset plate.

Module III

Compression members, effective length, slenderness ratio, types of cross-section, classification of cross section, Design of axially loaded compression members, lacing, battenning, design of column bases, and foundation bolts.

REFERENCES

Design of Steel structures

B.Tech, 6th Semester, CE

Books:

- [1] Limit State Design of Steel structures by S.K. Duggal, Mc-Graw Hill

CIVIL ENGINEERING

Design of steel structures

- Types of sections
- Grades of steel
- Strength characteristics
- IS code connections
- Design of tension & compression members
- Steel roof trusses, beams, column bases.

IRON

1. Pure iron (non alloy): →

- It is natural metal available directly in the market.
- silvery white in colour.
- It is very soft solid & such that it can be cut by knife, having high ductility.
- It is not used in any structural element since it directly reacts with oxygen & to form rust & reacts with moist air.
- It is available in Fe^{2+} & Fe^{3+} forms.

2. Pig iron: →

- Basic raw iron is called pig iron (transported in the form of bricks).
- It is also not used in any structural element since it is composed of highest carbon content (5%).
- the pig iron can be converted into structural iron by removing excess carbon content & by adding oxygen or chemicals in molten stage

3. Cast iron: —

- It is the structural element in specified shape from molten pig iron having almost same properties of pig iron.

4. Wrought Iron: →

- Lowest carbon content ($0.0-0.1\%$) of structural iron.
- It has high ductility, easily converted in specified shape.
- largely used to make thin wires.

5. Steel: →

- Steel is an alloy of iron + carbon + chromium + copper + magnesium + nickel + silica)

- the structural elements used to resist any type of load.

Carbon content

- Pig iron $\rightarrow 4-5\%$.

- cast iron $\rightarrow (2-4.5\%)$

- car steel $\rightarrow (> 2\%)$

\rightarrow carbon steel (less than 2%)

- High carbon steel $\rightarrow (0.6-1.4\%)$

- medium " " $\rightarrow 0.25-0.6\%$

- low " " \rightarrow less than 0.25% .

- Wrought iron - less than 0.1% .

- pure " $\rightarrow 0\%$.

Introduction

Properties	Low carbon	Medium carbon	High carbon
	Lower than 0.25% wt. %	In betn $0.25 \times 0.6\%$ wt. %	In betn $0.6 \times 0.7\%$ wt. %
carbon			
Some properties	<ul style="list-style-type: none"> - Excellent ductility & toughness. - Weldable & machinable - Not amenable to martensite transformation 	<ul style="list-style-type: none"> - Low hardenability - These steel grades can be heat treated. 	Hardest, strongest & least ductile.
Some appn	<ul style="list-style-type: none"> - Common products like Nuts, bolts, sheets, etc. 	<ul style="list-style-type: none"> - For higher strength such as in machinery, Automobiles & agricultural parts (gears, axles, connecting rods) etc. 	Used where strength, hardness & wear resistance is required. E.g. tool, musical wires.

→ Steel is an alloy of iron & carbon

MILD steel (carbon content = 0.23%)

- when carbon is increased in steel then strength, hardness & brittleness will increase, but ductility will decrease.

Stainless steel :-

- Alloy of iron & chromium.

- chromium is 18% & Nickel is 8%.

- Young's modulus of steel ' E ' = 2×10^5 MPa
 ≈ 200 GPa

$E_{\text{Aluminium}} \approx \frac{1}{3} E_{\text{Steel}}$

$$= 0.7 \times 10^5 \text{ MPa or } 70 \text{ GPa}$$

Density of steel:-

$$\dagger = \begin{cases} f_{\text{Steel}} = 7850 \text{ kg/m}^3 \\ f_{\text{Aluminium}} = \frac{f_{\text{Steel}}}{3} = 2700 \text{ kg/m}^3 \end{cases}$$

Modulus of Rigidity (G) :-

$$G = 0.769 \times 10^5 \text{ MPa}$$

Poisson's Ratio (ν) :-

$$\nu = \frac{\text{Lateral strain}}{\text{Longitudinal strain}}$$

- ν for mild steel = 0.28

- In elastic range = 0.3

- In plastic " = 0.5

Deflection / Increase in length :-

$$\Delta L = \frac{PL}{AE}$$

$$(\Delta L)_{\text{mild steel}} = \frac{1}{3} (\Delta L)_{\text{Al}}$$

Thermal Co-efficient :-

$$\alpha_{\text{Steel}} = \alpha_{\text{Concrete}} = 12 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$$

$$\alpha_{\text{Al}} = 23 \times 10^{-6} \text{ }^{\circ}\text{C}^{-1}$$

- Steel is ductile while concrete are brittle & brittle.

Note:-

Rubber is a very brittle material, there is very little plastic deformation beyond elastic range.

Some imp. codes

IS 456: 2000 → RCC

IS 800: 2002 → Steel (2007-LSM, 1984-WSM)

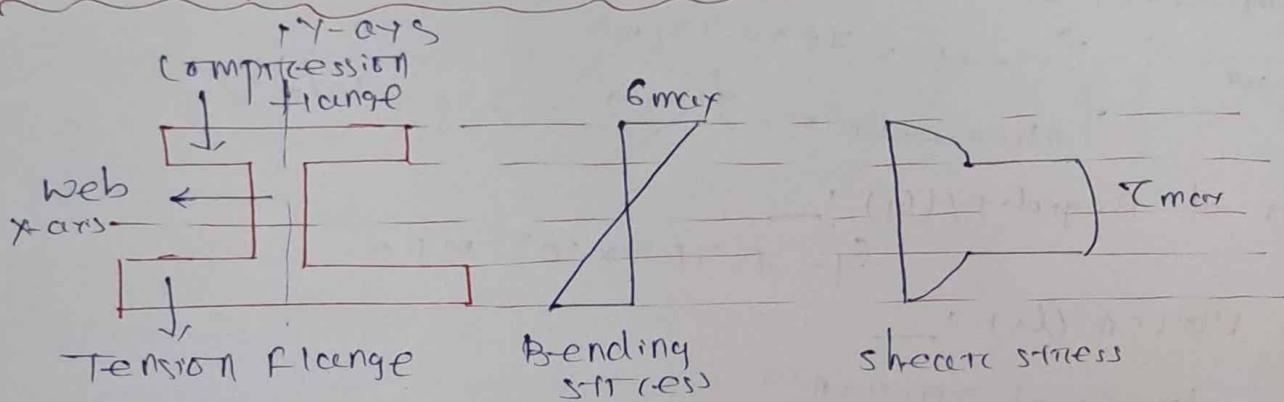
IS 1343 → Pre stress concrete

IS 10262 → Dgn. mix

IS 383 → Fine & Coarse aggregate

IS 825 → Dgn. load for buildings & structures.

Standard structural steel section



→ In I-sectn, the web resists sf while the flanges resist most of BM experienced by the beam.

i) ISLB 300:—
Indian standard light beam where overall depth = 300mm
- maxm bending stress is resisted by flange & maxm shear stress by web.
- Generally used in roof beam.

ii) ISMB:—
Indian standard medium flange beam generally used in floor beams.
- High moment of inertia about x-axis, so lateral buckling occurs about y-axis.

iii) ISWB:-

- Indian standard wide flange beam generally used in columns.

- High moment of inertia about y-axis, so they have bending strength about y-axis.

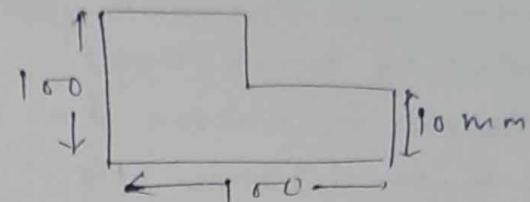
iv) ISJB:- Is junior beam

v) ISHB:- " Heavy "

Angle section

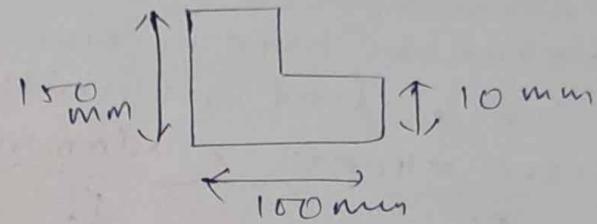
i) equal Angle sec": →

ISA - $100 \times 100 \times 10$
 Both legs
are same thickness
of angle sec



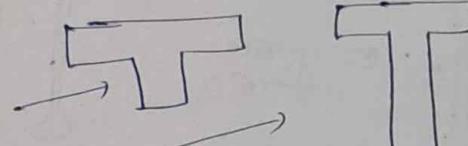
ii) unequal angle sec": -

ISA - $150 \times 100 \times 10$
 different legs thickness

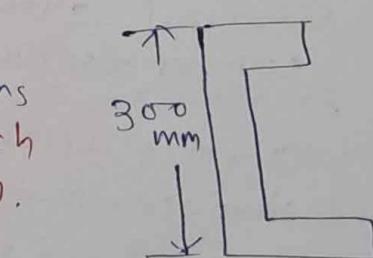


I-sec":

i) ISHT - Is wide flange I sec"



ii) ISST - Is short long legged I sec"



channel sec":

they were used as girders or columns
(girder is a beam in a roof truss which
supports the roof covering material).

i) ISJC - Is junior channel sec"

ii) ISLC - Is light "

iii) ISMC 300 - Is medium "

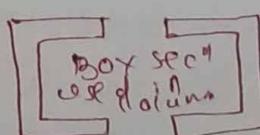
iv) ISSC - Is special "

BOX sec" - used in column

Flat sec":

ISF - Is flat sec"

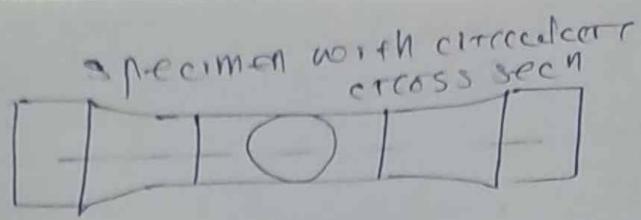
- used in dgn. of facing & batten.



Box sec
used in
columns

$$\text{Eq. } \sigma = \frac{F}{A} = \frac{F}{\frac{W}{t}} = \frac{Ft}{W}$$

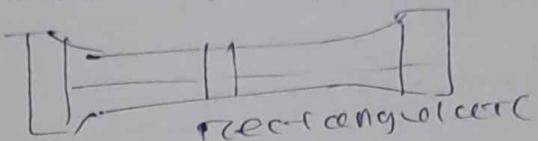
width of plate thickness of plate.



Uniaxial Tension Test:

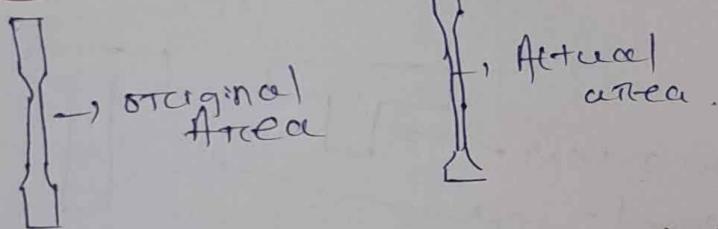
This test is of static type i.e. the load is increased comparatively slowly from zero to a certain value. A TM or OTC tensile testing machine is used.

- The ends of the specimen's ends secured in the grip of the testing machine.



- There is a device for applying a load to the specimen with a hydraulic or mechanical drive.
- There must be some recording device by which you should be able to measure the travel of the beam of load or stress.

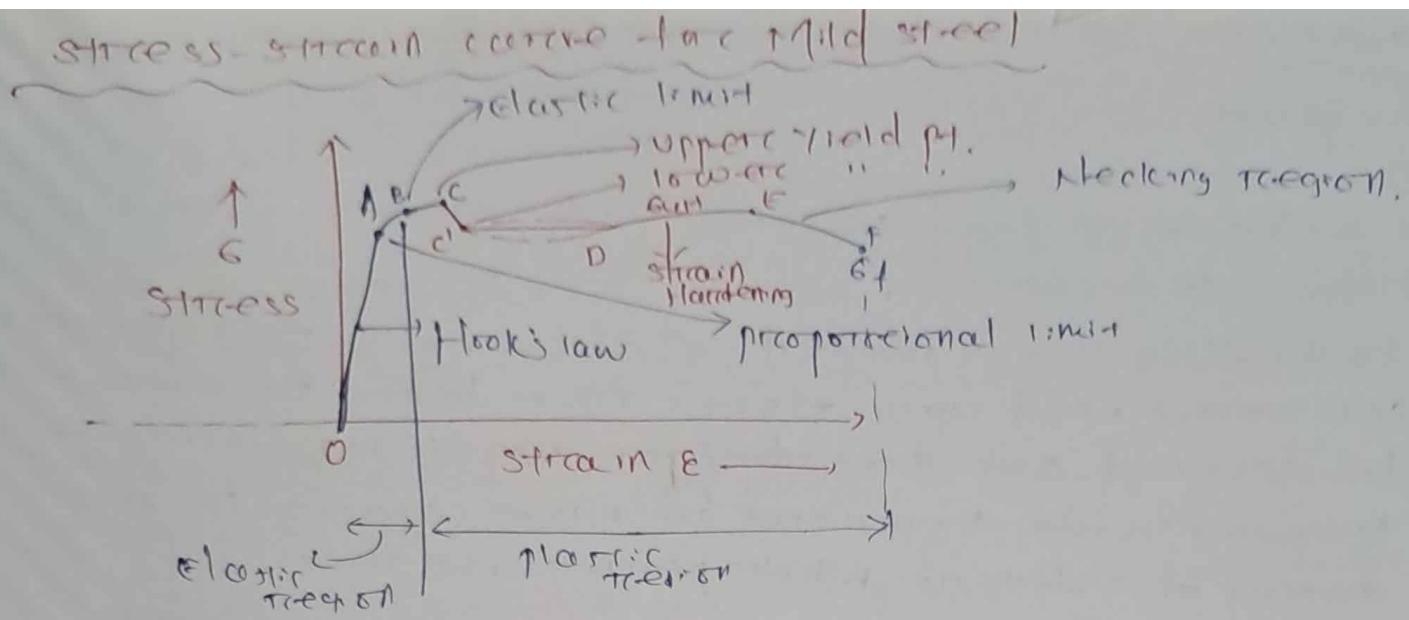
True stress & Nominal stress:



1. Nominal stress - Stress in OTC conventional stress - Stress in diagrams! → stresses are usually computed on the basis of the original area of the specimen; such stresses are often referred to as conventional or nominal stresses.

True stress - Stress diagram!

- Since when a material is subjected to a uniaxial load, some contraction or expansion always takes place. Thus, dividing the applied force by the corresponding actual area of the specimen at the same instant gives the so called true stress.



OA → Proportionality limit

OB → Elastic " But OB (non linear)

→ the slippage of the carbon atom with in a molecular mass
leads to drop down of stress marginally from C to C'.

→ C → Upper yield pt.
C' → lower " Yield stress f_y

For ex. Fe-250 $\Rightarrow f_y = 250 \text{ N/mm}^2$

→ C'D → const. stress region called yield plateau.

→ DE → Stress Hardening region \rightarrow material structures offering resistance against deform area.

→ EF → Necking region \rightarrow drop down of stress occurs upto failure pt.

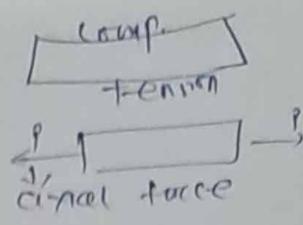
→ Necking region exists only in ductile material.

→ In mild steel - ABC come closer to each other, therefore it is known as linear elastic metal.
As yield stress & elastic stress is taken as 250 N/mm^2 .

→ The fracture or failure in mild steel depends upon
a) carbon present in a steel.

Permissible stress in steel structures

$$\left[\text{Permissible stress} = \frac{\text{Yield stress } f_y}{\text{FOS}} \right]$$



- F_c is the maxm load carried by the members without deformation.
- In working stress method, it is assumed that members can carry load upto elastic limit. Hence members will be designed such that they can resist less loads as compared to the resistance of maxm capacity by providing factor of safety to whole permissible stress.
- $\rightarrow \text{FOS} \rightarrow 1.67 \rightarrow$ for members s.t. Axial tension or comp.
 $\rightarrow 1.50 \rightarrow$ " " " Bending.
- since in axial loading all fibers reach max stresses, but in bending only extreme fibers will reach max stresses. Hence FOS will be less for bending.

Working stress Method:

- In the field there are always worst combination of loads (SL, LI, ENL, etc) hence members will be designed such that they can resist more & more loads of actuality if needed.
- Ultimately size & cross secⁿ area of the member increase. Hence working/failure stress decreases.
- Working stress =
$$\frac{\text{Load supplied to the members}}{\text{Cross sectional area}}$$

$$= \frac{\text{yield stress } f_y}{\text{FOS}}$$

Advantages:

- the members can be failed in fatigue having large life span.
- the dgn. is very simple.

Demerits:

- wt. of the str. increases, hence it is uneconomical.

Plastic Modulus or Limit State Method

- The dgn. of the members may reach the plastic regime i.e FOS will be desired to reach loads by considering load combinations x strength x serviceability requirements.
- Hence it is called as permissible factor of safety.
- Design load = $\frac{\text{corresponding characteristic load}}{\text{permissible factor of safety}}$

Permissible stress in steel \rightarrow 500 N/mm²

1 As per WSM:

i) max^m permissible axial stress in compression is

$$\sigma_{ac} = 0.60 f_y$$

- Used in the dgn. of columns & structures.
- column is a compression member where BM exists while in case of structures, also being a compression member, BM is zero. Because structures a component of roof trusses & roof trusses cut at pin jointed connection having BM = 0.

ii) max^m permissible axial stress in tension is given

$$\sigma_{at} = 0.60 f_y$$

- It is used in tension members.

FOS \rightarrow 1.67 \rightarrow axial tension & compression

- 1.50 - bending

iii) max^m permissible stress in compression is given! \rightarrow bending

$$\sigma_{bc} = 0.66 f_y$$

- Used in dgn. of flexural (bending) members i.e beam, built up beam, plate girders etc.

iv) max^m permissible bending stress in tension is

$$\text{given} \rightarrow \sigma_{bt} = 0.66 f_y$$

$$FOS = 2.5$$

v) max^m permissible avg. shear stress given, $T_{avg} = 0.40 f_y$

vi) " " " max^m " " " $T_{max} = 0.45 f_y$

$$FOS = 2.2$$

v) max^m permissible bending stress is given by:—
 $\sigma = 0.75 f_y$

Procedure of permissible stress! →

- When wind & earthquake load are considered, the permissible stresses in steel struc. are increased by 33.33%.
- " " , connections (rivets & weld) are ↑ by 25%.

Permissible deflection in steel struc.! →

→ max^m permissible horizontal & vertical deflection given
 → then $\delta = \frac{\text{Span}}{325}$ as per WSM

i) $\delta = \frac{\text{Span}}{300} \rightarrow$ supported elements are not susceptible to cracking

ii) $\delta = \frac{\text{Span}}{360} \rightarrow$ susceptible to cracking.

Permissible stress in Gantry girder! →

- Gantry girders are laterally unsupported beams to facilitate heavy loads from place to place at the construction sites.

i) For manuev'lty operator crane, $\delta = \frac{\text{Span}}{500}$

ii) For electrical " " , $\delta = \frac{\text{Span}}{750} \rightarrow$ upto 50T \downarrow 50TON capacity,

iii) " " " , $\delta = \frac{\text{Span}}{1000} \rightarrow$ more than 50T are 500kg

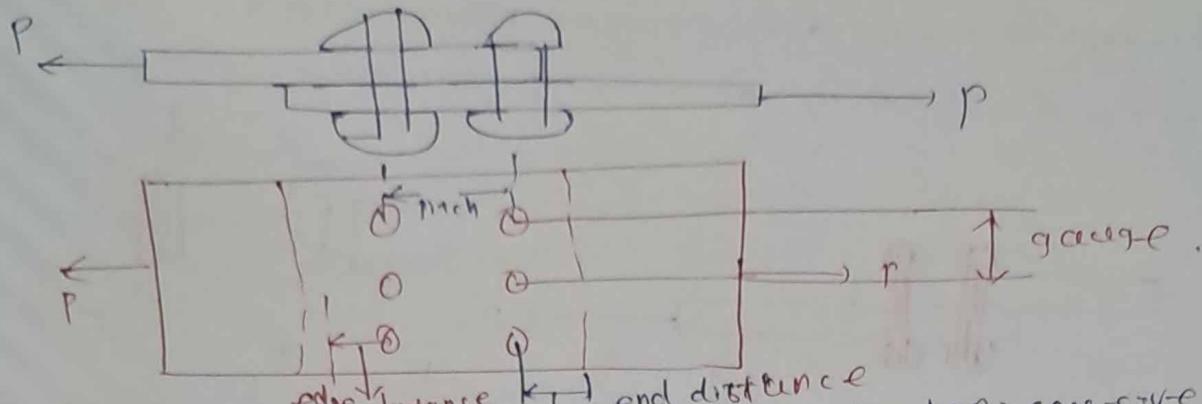
FOS for diff. stresses! →

$$\text{FOS} = \frac{f_y}{f} = \frac{\text{yield stress}}{\text{Working stress}}$$

Both tension & comp.

$$\hookrightarrow = 1.67 = \frac{f_y}{0.60f} \rightarrow \text{axial stress}$$

$$= 1.50 = \frac{f_y}{0.66f} \rightarrow \text{bending } "$$



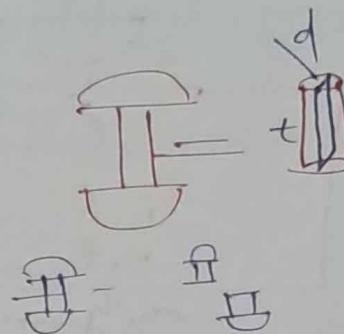
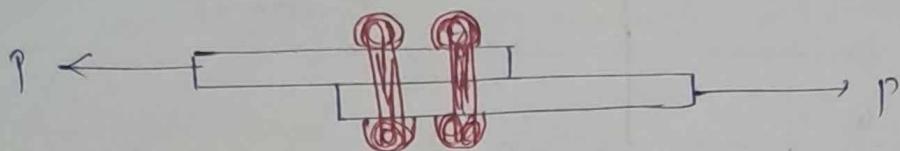
1. Pitch \rightarrow It is the distance between two consecutive continuous rivets measured parallel to the direction of force.
2. End distance \rightarrow It is the distance between centre of rivet & edge/end of the plate element, measured parallel to the direction of force.
3. Gauge distance \rightarrow It is the distance between two consecutive rivets measured parallel to the force of direction.
4. Edge distance \rightarrow It is the distance between centre of rivet & edge/end of the plate element, measured parallel to the force of direction.

Types of stresses

1. Direct stress
 - a) Direct tensile stress
 - b) " compressive "
 - c) " shear "
 2. Indirect stress
 - a) Bending stress $\rightarrow \frac{M}{I} = \frac{f_b}{Y} = \frac{E}{R}$
 - b) Torsional shear stress, $\frac{\tau}{T_p} = \frac{T}{I_p}$
- STRESS:- Normal \rightarrow Direct normal stress $\rightarrow \sigma_d = \pm \frac{P}{A}$
 Shear \rightarrow Bending $\rightarrow \sigma_b = \pm \frac{M}{I} Y$
 Primary shear stress $\rightarrow \tau = \pm \frac{f_a Y}{I_B}$
 Torsional " " $\rightarrow \tau = \frac{T}{J} \times r$

Bending stresses:

- It is nothing but compressive stresses developed at the surfaces of two different materials.
- Comp. force divided by characteristic area \rightarrow it.

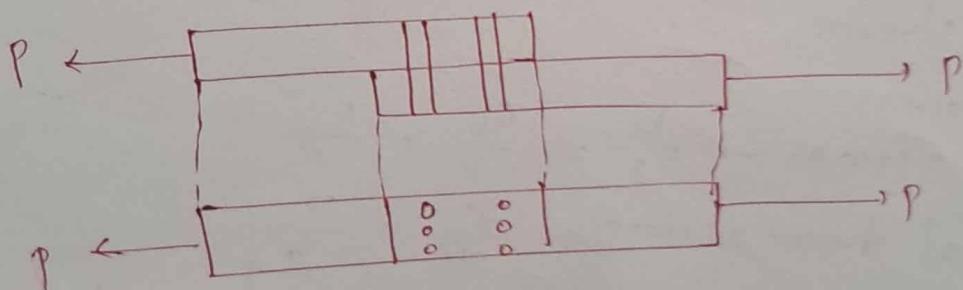


Shearing stresses:

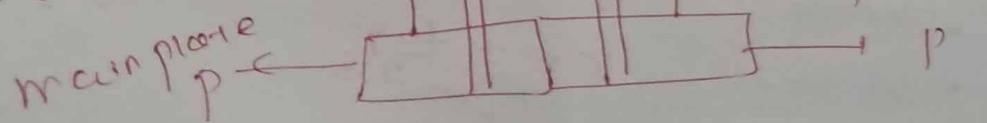
Two forces, equal & opposite in magnitude, which act tangential to the transverse secⁿ. as a result of which the body shears off across the secⁿ is known as shear stress.

Types of joints

1. Lap joint: → It is the least efficient joint as the line of action of two forces are not same.
In lap joint, the rivets are subjected to single shear & bending.
- These forces form couple & additional bending stresses are developed in the rivets.



2) Butt joint:



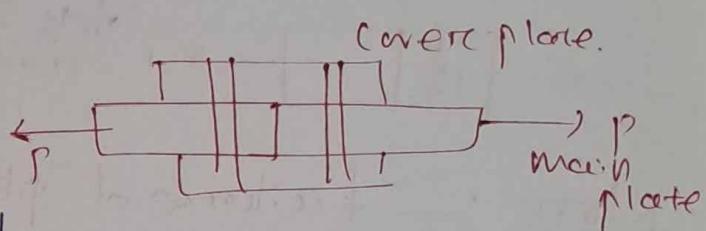
~~over bolt & joint~~

The line of action of two forces is same \rightarrow hence eccentricity is eliminated completely which existed in lap joint hence this joint is more efficient in carrying the force as compared to lap joint.

- But the connection is not symmetrical.
- the rivets are subjected to single shear & bearing.
- $t_{cover} \geq t_{main}$ (so that the joint doesn't fail).

Double cover butt joint:

- It is the most efficient joint because the line of action of two forces is same & connection is symmetrical w.r.t applied load.

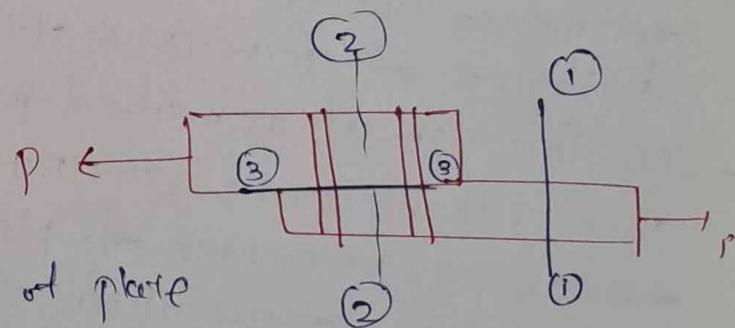


- the rivets are subjected to double shear & bearing.
- sum of thicknesses of cover plates $\geq t_{main}$.

Connections:

In steel str., various types of elements are connected together using various types of connections.

- i) Riveted connections
- ii) Bolted "
- iii) Welded "



Strength of plate:

sec' 1-1 \rightarrow Tearing strength of plate

sec' 2-2 \rightarrow Bearing " "

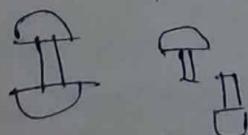
sec' 3-3 \rightarrow shear " "

Failure of Riveted joint

Failure of rivets

i) Shear

Rivet gets cut into two or more pieces.



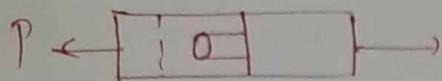
i) Bearing

- Rivet cross sec' changes from circular to elliptical.



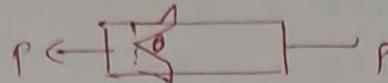
Failure of plates

i) Shearing



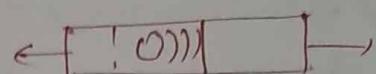
- occurs due to developed eccentricity due to the applied forces direction.

ii) Splitting



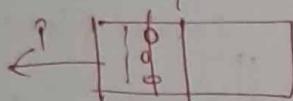
- It occurs due to diagonal tension in the plate at the rivet level

iii) Bearing



- this plate is pushed forward by the rivet. This type of failure occurs generally due to insufficient end distance.

iv) Tearing / tension failure of the plate:-



It is developed due to the direction of cracks or applied force.

Note :- Failure of plate:-

- shear, bearing & splitting failures of plate occur due to insufficient end distance.
- To providing the proper end distance, these three failure can be prevented.
- In the dyn. of riveted joint which should consider the remaining three failure only, i.e. shear & bearing failure of rivets & tearing failure of plate.
- In the dyn. of riveted joint, we have to ensure that, shear & bearing strength of rivets is more than the tearing strength of plate because rivet failure is more dangerous than the plate failure.

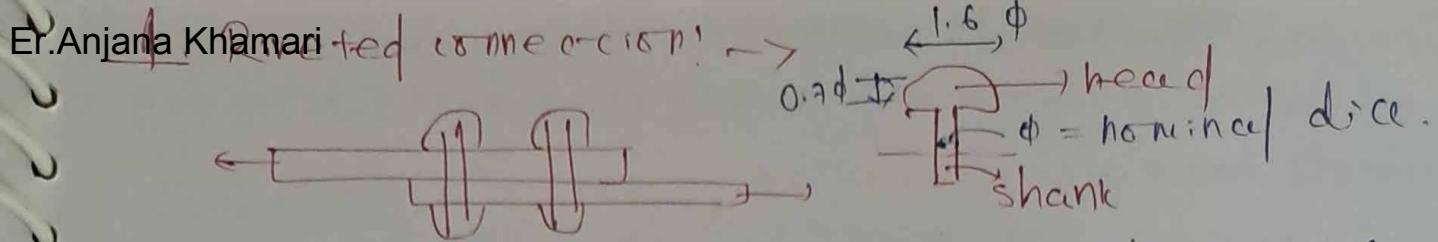
Plate:-

shearing	{	insufficient end distance
bearing		
splitting		

tearing

shearing	{
bearing	

Riveted



- Rivets are inserted in the hole made to join the two members together & hammering is done to make head on other side.
- Rivets are made of mild steel. The riveting can be hot riveting or cold riveting.
- cold driving is not adopted for $d:a > 10 \text{ mm}$.
- In " there is no gripping element but strength is better due to cold working.
- When hot rivet is used, it becomes plastic, it expands & fill the rivet hole completely in the process of forming a head at the other end. On cooling, the rivet shrinks in the length & due to shortening of " shank length.
- The connected part becomes lighter consequently resulting in tension of unpredictable amount in a shank length & some compression in plates that are connected.
- Due to reduction of dia. of shank on cooling, this small amount of space conceivable on cooling is provided for temp. variation of unpredictable amount.
- In hot riveting, rivets are heated to $550 - 1000^\circ\text{C}$ & hammering is done on other side to make head.
- According to the type of hammering we have:
 - i) power driven rivets
 - ii) Hand " "
- power driven rivets have better quality control & hence have a higher permissible stress.

~~Er. Anjana Khamari~~ can be done in the factory (or) in the field
X according to these hop riveting & field riveting
thus we have: —

- i) factory shop rivets PDS
- ii) " driven field " PDF
- iii) Hand " " " HDF

if true

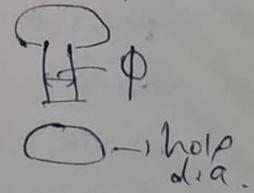
Note

For shop rivet

For field rivet ○

N/mm ²	Axial tension	shearing	bending
PDS	100	100	300
PDF	90	90	270
HDF	80	80	250

- the nominal dia of rivet is said to be shank dia under cold condn & gross dia. of rivet is taken as dia of hole.
- the strength of a rivet is based on its gross dia. center
- the assumption that rivet fills the hole completely.
- For ease in connection dia. of hole is taken larger than nominal dia. of rivet thus as per IS: code: —
- For $\phi \leq 25\text{ mm}$
 - gross dia = $\phi + 1.5\text{ mm}$
 - dia. hole = $\phi + 1.5$
- For $\phi > 25\text{ mm}$
 - gross dia. = $\phi + 2\text{ mm} = \text{dia of hole}$
- Due to many demerits, riveted connection is not in practice in modern steel connection.



$$\begin{aligned} \text{if } \phi = 16\text{ mm} \leq 25\text{ mm} \\ \text{hole dia} &= 16 + 1.5 \\ &= 17.5\text{ mm} \end{aligned}$$

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rigid riveted connection is same as that of bolted connection but with the following differences:

- i) the dia. of rivets to be used in the riveted connection is dia. of hole, whence as in bolted connection it is the nominal dia.
- ii) the dgn. stresses are different (IS: 800 : 1984) the permissible stresses are reduced for bolts.

Strength of riveted joint:

τ_c is taken as min. of shear strength, bearing & tearing strength.

For lap joint:

- i) For entire plate:

- a) shear strength of rivets

$$P_s = n \times \frac{\pi}{4} \times d^2 \times f_s$$

whence,

$n \rightarrow$ total no. of rivets at joint

$f_s \rightarrow$ permissible shear stress in rivets

$f_u = 150 \text{ MPa (WSM)}$

$F_u = \text{Ultimate shear stress in rivet}$

$$\text{so in L.S.M.} = \frac{F_u}{\sqrt{3} \times 1.25}$$

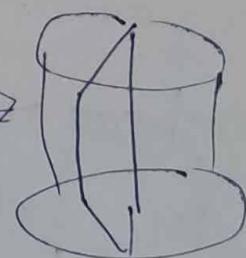
$d = \text{gross dia. of rivet + hole dia.}$

$\text{gross dia.} = \phi + 1.5 \text{ mm}, \phi \leq 25 \text{ mm}$

$= \phi + 2 \text{ mm}, \phi > 25 \text{ mm}$

- b) bearing strength of all rivets

$$P_B = n \times (t \times d) \times f_b$$



where,

$t = \text{thickness of thinner main plate.}$

$f_b = \text{permissible shear stress in rivets}$
(300 MPa in WSM)



$d+gr$

Er. Anjana Khamari

$$P_c = (B - n, d) t \times f_t$$

where,

n → total no. of rivets act. sec

B → width of the plate

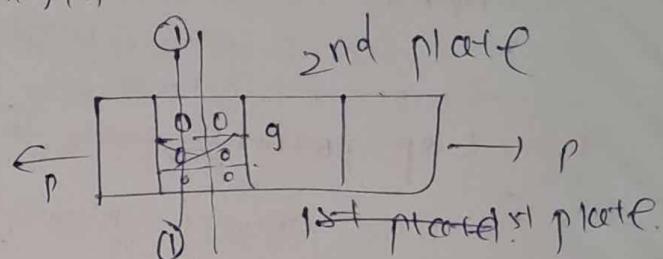
f_t → permissible tensile stress in rivets

$$(Axial = 0.6 f_y = 0.6 \times 250 = 150 \text{ MPa})$$

i) For Gauge length / Pitch length

a) shear strength of rivets

$$P_{S1} = n \times \frac{\pi}{4} \times d^2 \times f_s$$



n → total no. of rivets act. joint in crossed gauge length

~~$f_s = \text{pitch}$~~

b) Bearing:

$$P_{B1} = n, t \times d \times f_b$$

c) Tearing:

$$P_{T1} = (g - d) \times t \times f_t$$

when pitch distance is given then $P_c = (p - d) t \times f_t$
 g → gauge length.

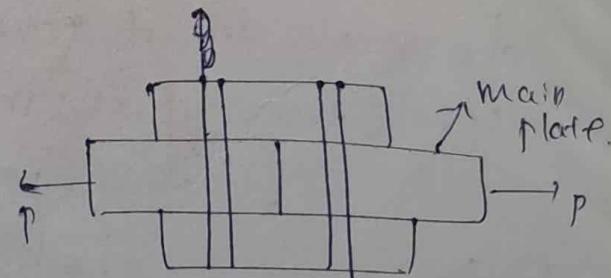
Double cover butt joint →

i) For entire width of plate

a) shear strength of rivets

$$P_{S1} = 2 \times n, \frac{\pi}{4} \times d^2 \times f_s$$

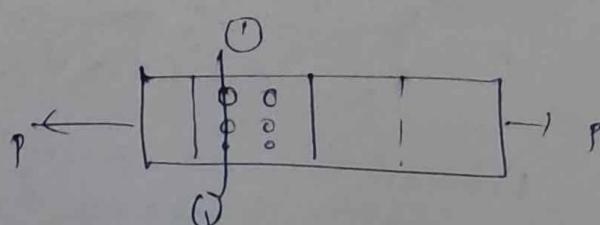
↳ double shear



b) bearing strength of rivet

$$P_B = n \times (t \times d) \times f_b$$

↳ min of (thickness of thinner main plate, sum of cover plate thickness)



Riveting Strength

$$P_r = (B - n \cdot d) t \times f_t$$

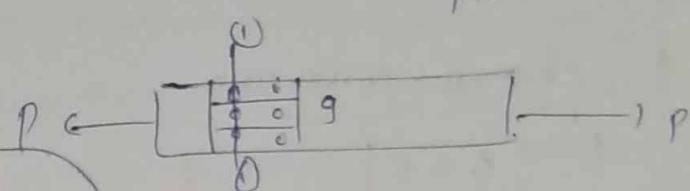
n → total no. of rivets at critical section
 t → min of (thickness of thinner main plate, sum of cover plate thickness)

Hence $- n = \frac{\text{total no. of rivets}}{\text{cross}}$

i) For Gauge length

a) shear: —

$$P_s = 2 \times n \times \frac{\pi}{4} \times d^2 \times f_s$$



$n = \frac{\text{total no. of rivets at joint in crossed gauge length}}{\text{length (hence 2)}}$

b) bearing: —

$$P_b = n \times (t \times d) \times f_b$$

c) tearing: —

$$P_t = (g - n \cdot d) t \times f_t$$

thickness of thinner main plate

n → total no. of rivets at in critical section in crossed gauge length (hence 1)

* No. of rivets required at a joint, $= \frac{\text{total force at joint}}{\text{Rivet value}}$

$$\Rightarrow n = \frac{F}{R_v}$$

* efficiency of joint, $\eta = \frac{\text{least value of } P_s, P_b, P_t}{\text{strength of solid plate}} \times 100$

P_s = shearing strength of joint

P_b = bearing " " "

P_t = tearing " " plate

* efficiency of entire plate! —

We have to ensure that P_t is less because rivet failure is more dangerous.

For entire plate! —

$$\eta = \frac{\text{least value of } P_s, P_b, P_t}{\text{strength of solid main plate}} \times 100$$

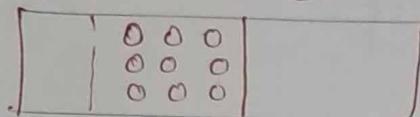
$$= \frac{(B - n \cdot d) \times t \times f_t}{B \times t \times f_t} \times 100 = \frac{(B - n \cdot d)}{8} \times 100$$

For gauge length:

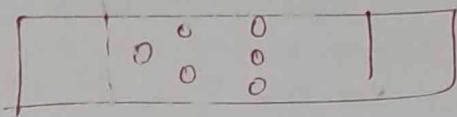
$$\eta = \frac{(g-d) \times t \times f_t}{g \times t \times f_t} \times 100 = \frac{g-d}{g} \times 100$$

Arrangement of rivets

1. chain riveting



2. diamond



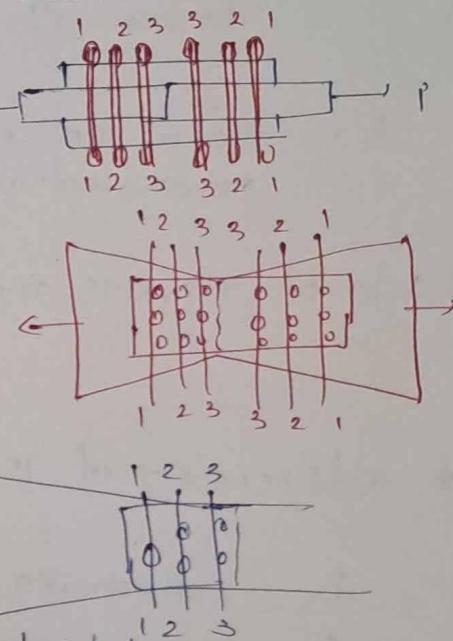
- In chain riveting the rivets are arranged as shown:-
- 1-1, 2-2 & 3-3 shows sec's in either side of the joint.
- 1-1 → central sec/main plate → outer most sec'
- 3-3 → " " of cover " " → inner " "

Strength of main plate:-

$$P_{1-1} = (B - 3d) \times t \times f_t$$

$$P_{2-2} = (B - 3d) \times t \times f_t + 3R_v$$

$$P_{3-3} = (B - 3d) \times t \times f_t + 6R_v$$



Strength of cover plate:-

$$P_{3-3} = (B - 3d) \times t \times f_t$$

$$P_{2-2} = (B - 2d) \times t \times f_t + 3R_v$$

- In diamond pattern:-

sec 1-1, 2-2 & so on has to be checked

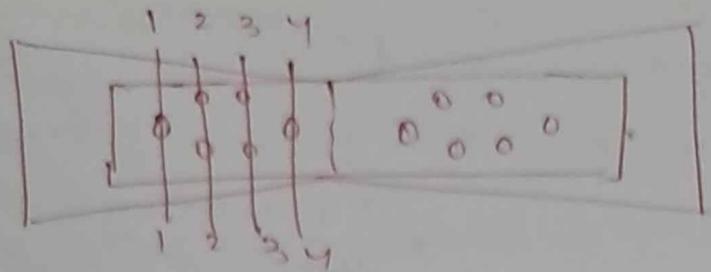
for main plate in carrying a required load, but for cover plate the last sec is checked for carrying a required load.

Strength for main plate:-

$$P_{1-1} = (B - d) \times t \times f_t$$

$$P_{2-2} = (B - 2d) \times t \times f_t + R_v$$

$$P_{3-3} = (B - 3d) \times t \times f_t + 3R_v$$



- Parallelogram sequence pattern of riveting. Section 2-2 is checked for main plate in carrying a transverse load.
- For cover plate, 4-4. Main plate or 1st seen for cover plate is supposed to be checked for cover plate, also sec 3-3 & 2-2 is also checked for safety.

Strength for main plate:-

$$P_{1-1} = (B-d) \times t \times f_t$$

$$P_{2-2} = (B-2d) \times t \times f_t + R_v$$

$$P_{3-3} = (B-2d) \times t \times f_t + 3R_v$$

$$P_{4-4} = (B-d) \times t \times f_t + 5R_v$$

(Prevision is valid for
Machine cut element)

Specifications As per IS 800-1984:-

min end & edge distance = 1.5 x gross dia. of rivet

- this recommendation is intended to prevent 3 types of failure in plates:-

i) splitting failure of plate

ii) shearing " " "

iii) bearing " " "

→ For head obscured elements:-

min (edge distance + end distance) = 1.7 x gross dia. of rivet

→ But for analysis & design purpose
 $= 2 \times$ gross dia. of rivet.

Pitch

- Min pitch of rivets $\approx 2.5 \times \phi$ \rightarrow nominal dia of rivet \rightarrow thickness of thinner plate
 - Maxm pitch \approx " or width \rightarrow thickness of thinner plate
- | | |
|-----------------------------------|-------------------|
| <u>In compression</u> | <u>In tension</u> |
| 12t or 200 mm | 16t or 200 mm |
| = 108mm or 300 mm
(min of two) | (min of two) |
- The maxm pitch provision is provided to ensure the prevention of buckling behind the connection.
 - The maxm pitch provision is provided to ensure the prevention of separation of plates behind connection.

Note

If the rivets are staggered (not in the same line) & the gauge distance smaller than 75 mm, then above recommended values in comp. & tension zone the maxm pitch are increased by 50% i.e.,

For comp.

$$\text{maxm pitch} = 18t \text{ or } 300 \text{ mm}$$

(min)

For tension

$$= 24t \text{ or } 300 \text{ mm}$$

(min)

* Gauge length (g) \rightarrow $\nexists 100 + 4t$ or 200 mm
maxm edge distance should not exceed 12t &

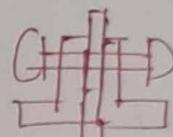
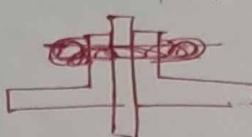
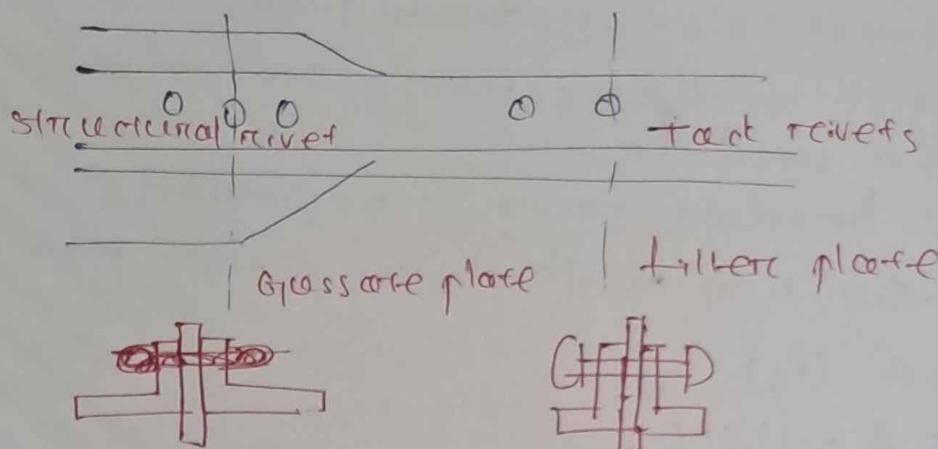
where, $E = \sqrt{\frac{250}{t}}$

- When the members are exposed to corresponding maxm edge distance should not be greater than $40 + 4t$.

Tack rivets

they are the rivets used to make the structural component as a single unit.

- they don't carry any load because we consider tack rivets not as a structural unit i.e provided as the location of gussete plate.



- The max^m pitch provided in the case of tack rivets when two angle seats were placed back to back to gussete plate as:

- 1000mm in case of tension { Both valid for
angle & channel
seats }
- less than 600m - comp.

- * When two plates are connected to a gussete plate back to back, then the max^m pitch is taken as
- 32+ or 300mm (min.)

Unwin's formula

$$\phi = 6.04 \sqrt{t} \quad \text{thickness of thinner plate}$$

- It is used where dia of rivet is not 16mm.

Note

- for field rivet, the permissible stress is reduced by 10%
- the permissible stress in rivet under wind load condn as per IS800 can be ↑ by 25%.
- " " " under wind & earthquake load condn ↑ by 25%.

- When thickness of concrete plates is not given, then the thickness of concrete plate should not be $\leq \frac{5}{8}$ times (thinner)

Assumptions in dgn. of riveted joint

- The applied axial load is assumed to be shared by all the rivets equally.
- The tensile stress ($0.6 f_y$), shear stress ($0.4 f_y$) & bearing stress at the toe of the rivet are assumed to be uniform.
- The effect of bending stress is neglected.
- Grip length is the sum of thickness of two plates.
 - i) Grip length (l_g)
 $l_g \geq 5\phi \rightarrow \text{LSM}$
 - ii) $l_g \geq 8\phi \rightarrow \text{WSM}$
- The friction force between the plates is neglected.
- $(g-d) \cdot f_f \leq n R_v$ (most imp. consideration).

- ① Steel is mainly an alloy of \rightarrow Iron & carbon
- ② Disadvantage of steel \rightarrow Friction & corrosion resistance
- ③ Elastic modulus of steel $\rightarrow 2 \times 10^5 \text{ N/mm}^2$
- ④ Unit mass of steel $\rightarrow 7850 \text{ kg/m}^3$
- ⑤ Poisson's ratio of steel $\rightarrow \frac{0.3}{}$
- ⑥ Structural steel normally has carbon content less than $\rightarrow 0.6\%$.
- ⑦ When manganese is added to steel \rightarrow improves strength & hardness of steel
- ⑧ Properties of high carbon steel \rightarrow reduced ductility
- ⑨ minm % of chromium & nickel added to stainless steel $\rightarrow 0.5\% \text{ to } 10.5\%, 0.5\%$

- (10) the effect of increase content of sulphur & phosphorous in steel → affects weldability.
- (11) correct criterion to be considered while designing:—
structure should be adequately safe, should have adequate serviceability.
- (12) serviceability:— It means that the structure should perform satisfactorily under different loads without discomfort to user.
- (13) Analysis → determination of axial forces, BM, S.F etc.
- (14) mainly adopted for design of steel struc. as per IS code → limit state Method
- (15) general construction of steel → IS 800
- (16) permissible stress = $\frac{\text{yield stress}}{\text{FOS}}$.
- (17) In WSM,
working stress \leq permissible stress
- (18) $\boxed{\text{load factor} = \frac{\text{ultimate load}}{\text{Working load}}}$
- (19) the eff. length of a compression member of length 'L' held in position & restrained in dirn at one end & effectively restrained in dirn but not held in position at the other end is → L
- (20) $\frac{\text{load factor}}{\text{Inelastic limit}} = \frac{\text{shear stress}}{\text{shear strain}} = \text{shear modulus of elasticity}$
- (21) A beam is defined as a structural member s.t
→ transverse loading
- (22) A riveted joint can fail in → $\left\{ \begin{array}{l} \text{tearing of plate only} \\ \text{shearing of rivet} \\ \text{bearing of " } \end{array} \right.$

(23) Gross dia = 14 mm \leq 25 mm.

$$d = d + 1.5 \leq 14 + 1.5 = 15.5$$

The gross dia. of a 14 mm nominal dia rivet is 15.5 mm.

(24) The strength of field rivets as compared to shop rivets is $\sim 90\%$.

(25) The maxm c-to-c distance b/w rivets in a tension member of thickness 10 mm is ~ 160 mm

(26) min pitch of rivets shall not be less than (where d is gross dia of rivet) $\rightarrow 2.5d$

2. Bolted connections

- A bolt is a metal pin with a thread at one end & a shank's threaded at the other end to receive a nut.
-
- shank
 area (A_{sb})
 at the root
 of thread
 $(A_{fb} = 0.78 A_{sb})$

Types of Bolts

- ① Black bolt / ordinary bolt / unfinished bolts: -
- It is the least expensive bolts, used for light str. s.t. static loads & for secondary members such as purlins, bracing etc.
 - They are not recommended for connections s.t. impact load, vibration & fatigue.
 - The bolts are available from 5mm to 36mm in dia & are designated as M5 to M36.

- Bolt of property class 4.6 means:
- i) ultimate strength of bolt (f_{ub}) = 400 MPa
 - ii) yield " " " " " $(f_{yb}) = 0.6 \times 400 = 240$ MPa
 - iii) yield " " " " " $(f_{yb}) = 0.6 \times 400 = 240$ MPa

- ② Torched bolts / close tolerance bolts: -
- It has small tolerances & are used in no slip connection. They are mainly used machines & under dynamic loading cond's.

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Types of bolted joints:-

1. Lap joint.

1. single bolted lap joint
2. Double " "

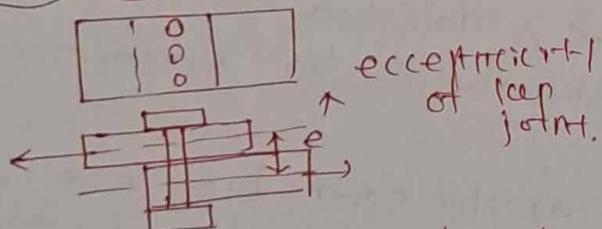
2. Butt joint.

1. Double cover single bolted butt joint
2. " " double " "
3. single " single " "

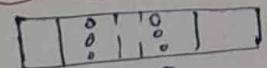
3) High strength bolt

- they are available from 16 mm to 36 mm in diameter.
- the most commonly used bolts are of 8.8 class (or) 10.9 grade class. 8 → stands for high strength.
- these bolts may be tightened until they have maximum high tensile stresses so that the connected plates are tightly clamped together between the bolt heads & nuts & friction developed between the plate surfaces s.t. clamping force.
- developed between the plates with specified initial tension value.
- the high strength bolts with specified initial tension value known as high strength friction grip (HSFG) bolt.

single bolted lap joint

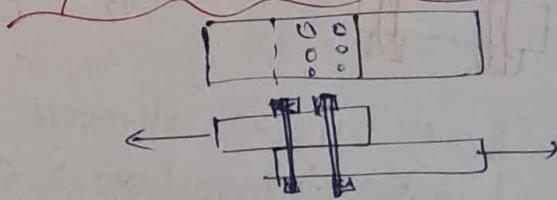


double cover single bolted butt joint

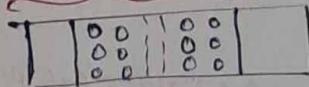


Types of bolted joints

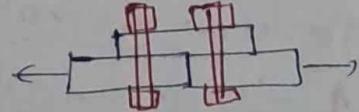
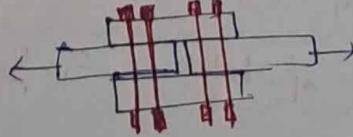
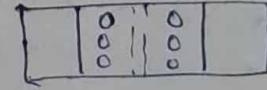
Double bolted lap joint



double cover double bolted butt joint



single cover single bolted butt joint



- double cover butt joint eliminates the eccentricity hence bending is eliminated.

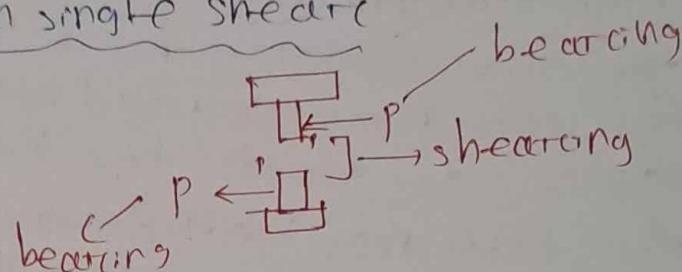
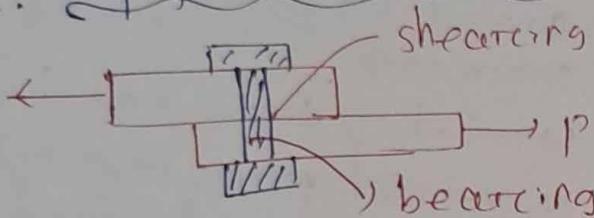
- the load in the lap joint has eccentricity hence a couple is formed which causes undesirable bending in the connection & bolts may fail in tension.

- to minimize the effect of bending in lap joints atleast bolts in a line must be provided.

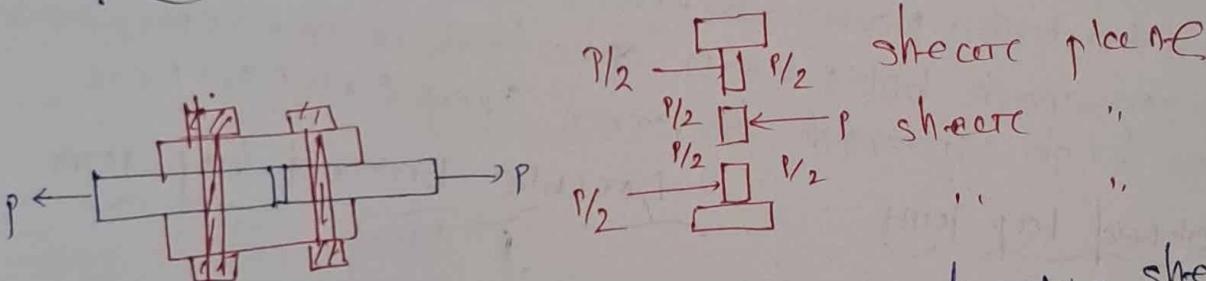
Load Transfer Mechanism

- Load transfer from one connected part to another depends on the type of connection.
- In bearing type connection, using ordinary bolts, the load transfer is by shearing & bearing.
- In slip critical / slip resistance connection, using HSFG bolts, the load transfer by friction.
- Transfer of forces in lap joint & butt joint

1. Lap joint, bolts are in single shear



2. Butt joint, bolts are in double shear!

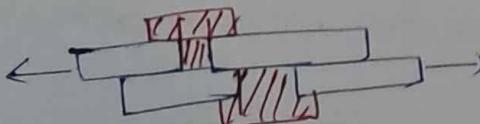


→ Bolts with single shear plane & double shear plane are called single shear bolt & double shear bolt respectively.

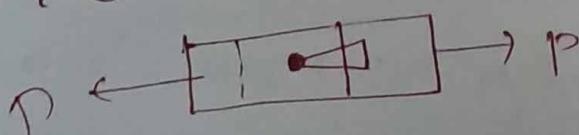
→ Shear capacity of a bolt in a double cover butt joint is double that of a bolt in a lap joint because of two shear planes.

Failure of bolted connections

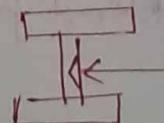
1. Shear failure of bolts



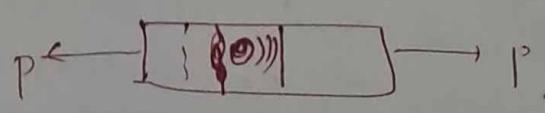
2. Shear failure of plates

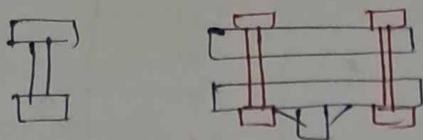
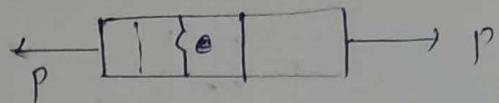
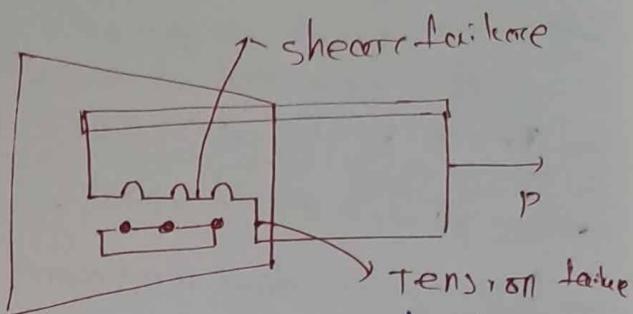
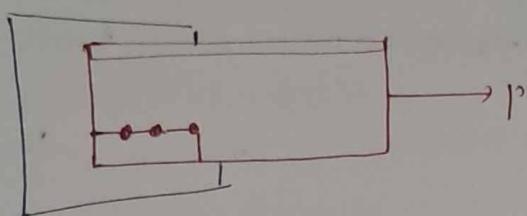


3. Bearing failure of bolts



4. Bearing failure of plates



5. Tension failure of bolts6. Tension failure of plate7. Block shear failure

→ It is a limit state that combines tensile failure on the plane & shear failure on another plane.

→ Block shear failure may occur when material bearing strength & bolt shear strength is high.

specifications of bolted connections1. dia. of bolt holes:

→ Under normal situation, dia of bolt hole is made larger than the shank area to facilitate extraction.

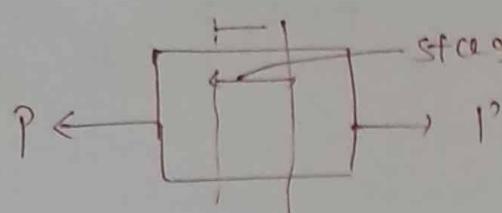
nominal dia of bolt	in mm					
	12mm	14mm	16mm	20mm	24	30 36
dia of hole	13	15	18	22	26	33 39
	+1 mm	+2 mm	+3 mm			

Q In calculating the area to be deducted for bolts of 36 mm dia, the dia. of hole shall be taken

as → 36 mm - nominal dia. $\rightarrow \phi > 24 \text{ mm}$

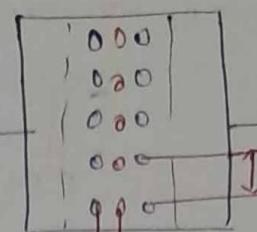
$$\text{dia. of hole} = 6 + 3 \text{ mm} = 36 + 3 = 39 \text{ mm}$$

2. Pitch (P) & Gauge (g)



staggered pitch P

P'



P

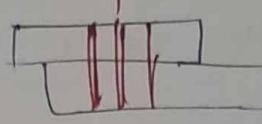
g

\rightarrow min^m pitch & gauge = 2.5 d

d = nominal dia. of bolt

\rightarrow pitch is the distance b/w two consecutive holes in

the direction of force.



"

" 1C to

\rightarrow Gauge is the distance " " " the direction of force.

- Bolts are kept apart at a sufficient distance & a min^m pitch is ensured due to:
 - to prevent bearing failure of members b/w the two bolts.
 - to permit eff. installation of bolts.
- max^m pitch
- It is desirable to place the bolts sufficiently close together for the following reasons:-
- To reduce the length of connection & gusset plate i.e., to have a compact joint.
- To have uniform stress in bolts.

1. For tension members $\rightarrow P \neq 16t$ or 200mm

$\rightarrow P \neq 12t$ or 200mm

2. For comp.

3. For rows near the edge $\rightarrow P \neq 4t + 100\text{mm}$ or 200mm

4. staggered pitch - When the gauge doesn't exceed 25mm, the pitch in 1, 2, 8, 3. may be increased by 50%. when bolts are regularly staggered.

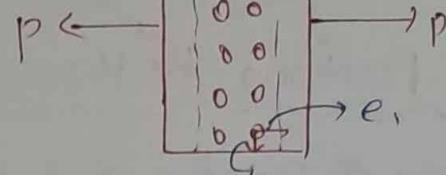
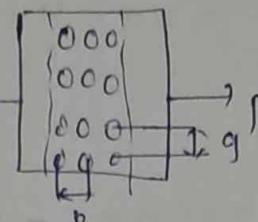
5. max^m gauge $\rightarrow g \neq 32t$ or 350 mm

max^m pitch

Note

For wide plates, pitch is defined as centre to centre distance of bolts measured along the length of the connection.

Pitch (p) & Gauge (g)
maxm pitch



e_1 → edge distance
 e_2 → end "

- It is assumed that the load on the joint is shared equally among all the bolts, in short length joints
- the force in bolts will be redistributed by plastic action & hence the bolt will share load equally.
- However in long joints (> 15 times dia. of bolt) the shear deformation is not uniform.
- the bolt at the ends of the joints are heavily stressed resulting in a progressive failure called 'unbuttoning'. Thus a compacting joint is desirable.

(3) Edge & End distance

- distance from the centre of bolt hole to the adjacent edge of the member at right angles to the direction of stress is called edge distance.
- distance from the centre of bolt hole to the adjacent edge of the member in a direction of stress is called end distance.
- Bolt holes should not be placed too near the edge due to:
 - i) the failure of plate in tension may be false place.
 - ii) the steel of the " opposite to the hole may be budge & crack.
- $\rightarrow \text{Min}^m \text{ end or edge distance} = 1.7 d_o$
(for sheared or hand flame cut edges).
- $\rightarrow \text{Min}^m \text{ end or edge distance} = 1.5 d_o$
(for machine cut & planed edges)
- $d_o = \text{d.o. of bolt hole}$
- $\rightarrow \text{Max}^m \text{ end or edge distance} = 12 + \epsilon$
 $\epsilon = 200\sqrt{250/f_y}$, $t = \text{thickened at thinner plate}$

- When the members are exposed to corrosive environment, maxm edge distance $\geq 40 \text{ mm} + 4t$.

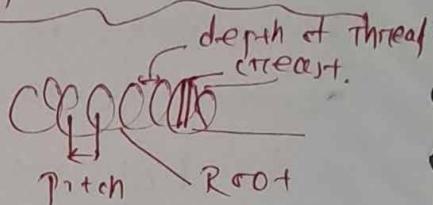
Tacking Bolts

- maxm pitch = $32t$ or 300 mm → when plates are not exposed to weather.
- $= 16t$ or 200 mm → " " " exposed to weather

* for two members placed back-to-back, the maxm pitch of tacking bolts $\geq 1000 \text{ mm}$.

(154) Assumptions in the calculations of simple bolted joints

- friction betw the plates is neglected & load is resisted by bolts, in bending & shearing.
- In case of bolts if threads occurs in the plane of shear, the eff. area resisting shear is taken as the area on the root of thread.
- However if " don't occur in plane of shear, eff. area is the cross-section area of the shank.
- the applied load is equally resisted by all the bolts.
- Distribution of stress on the portion of plate b/w the bolt holes is uniform, i.e., stress conc. around the hole is neglected.
- this assumption is made for ease in calculation. However at the time of collapse this assumption would be actually valid.
- * the bending stress in the bolt is neglected.
- * " " " is assumed to be uniform over the nominal contact area b/w the plate & bolts.



Strength of bolt in bearing type connection

$$\text{Dgn. strength of bolt} = \min \left\{ \begin{array}{l} V_{dsb} \\ V_{dpb} \end{array} \right\}$$

Dgn. shear strength of bolt
" bearing " "

$$V_{dsb} = \min \left\{ \begin{array}{l} V_{dsb} \\ V_{dpb} \end{array} \right\}$$

$V_{dsb} = \frac{V_{nsb}}{\gamma_{mb}} \rightarrow$ Nominal shear strength of bolt
 $\gamma_{mb} \rightarrow 1.25 \rightarrow$ material safety factor for material

$$V_{dpb} = \frac{V_{npb}}{\gamma_{mb}} \rightarrow \text{nominal bearing strength of bolt}$$

For safety,

$$V_{sb} \leq V_{db} \text{ (also called bolt value)}$$

↳ Factor shared load in one bolt.

A) Shear strength of bolt

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (n_n A_{nb} + n_s A_{sb}) B_{sj} B_{lg} B_{pk}$$

Where,

$$V_{dsb} \rightarrow \text{Dgn. shear strength of bolt}$$

$f_{ub} \rightarrow$ ultimate

$\gamma_{mb} \rightarrow 1.25$

$n_n \rightarrow$ no. of shear planes with threaded material across the shear plane

$n_s \rightarrow$ " " " without " " " "

$A_{nb} \rightarrow$ net tensile area of bolt (ET) area of the root of threaded = $0.78 A_{sb}$

$A_{sb} \rightarrow$ nominal shear area of bolt.

$B_{sj}, B_{lg}, B_{pk} \rightarrow$ Reduction factors taking into the effect of long joints, large grip length & packing plates.

for single shear case:-

$$V_{dsb} = \frac{f_{cb}}{\sqrt{3} \times 1.25} (1 \times A_{nb})$$

- Unless specified V_{dsb} would be calculated corresponding to shear plane intercepting the threaded.

for double shear case:-

$$V_{dsb} = \frac{f_{cb}}{\sqrt{3} \gamma_{mb}} (1 \times A_{nb} + 1 \times A_{sb})$$

- Under the assumption that one of the shear plane is intercepting the root of threaded & other is intercepting the shank.

B) Bearing strength of bolt

$$V_{dpb} = \frac{N_{pb}}{\gamma_{mb}}$$

$$= 2.5 \times k_b \times d \times t \times f_u$$

Whence,

 d = nominal dia. of bolt t = summation of thickness of plate elements experiencing bearing in same direction 2.5 is const. whose value corresponds to hole elongation about 6mm.

$$k_b = \min \left\{ \frac{e}{3d_0}, \frac{P}{3d_0} - 0.25, \frac{f_{cb}}{f_u} \times 1 \right\}$$

 e → end distance P → pitch d_0 → dia. of bolt hole f_{cb} → ultimate strength of bolt f_{cp} → ultimate strength of plate.

→ Bearing failure in the bolts is possible only if the bolts used are of very low grade & plate joint are of high grade which is not possible.

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The bearing strength of bolted connection is a form of strength of connected plates & the arrangement of bolts is other than cascade of bolts.

- the bearing strength is also a form of bolt hole.
- the " " is calculated where there is two standard bolt holes, for oversized & short slotted holes it is 0.7 times the bearing strength & for slotted holes it is 0.5 times of the " " .

c) Tensile strength of bolt

$$T_{db} = \frac{T_{nb}}{\gamma_{mb}} = \frac{0.9 f_{ub} A_{nb}}{1.25} \rightarrow \text{net tensile area of bolt} = 0.78 A_{sb}$$

$$T_{db} \leq \frac{f_{yb} A_{sb}}{\gamma_{mo}} \rightarrow 1.1$$

(161) Dgn. strength of plate

- the plate may fail by:-

i) shearing of plate! -
It can be avoided by keeping sufficient edge distance.

ii) yielding of plate! -
For gross secⁿ yielding! - $T_{dg} = \frac{f_y A_g}{\gamma_{mo}} \rightarrow 1.1$
dgn. tensile strength \downarrow
in gross secⁿ yielding

iii) Reapture of plate! -

for net secⁿ reapture! - $T_{dn} = \frac{0.9 f_u A_n}{\gamma_{m1}}$

Where,

T_{dn} = dgn. tensile strength in reapture.

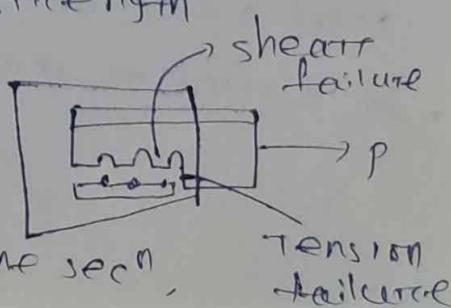
A_n = eff. net area of secⁿ

- factor 0.9 is introduced as there is no reserve strength beyond ultimate strength

iv) Block shear failure! -

- When a block material within the bolted area breaks away

- from the remainder portion of the secⁿ.



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- surface is formed as block shear interface.
 - this occurs along a path involving tension in the plate & shear on a 45° plane.
 - It occurs, one of the surfaces (stronger one) fractures while the other yields.
 - yielding occurs on gross area while fracture on net area.

$$T_{db} = \min \left\{ \begin{array}{l} \text{shear yielding} + \text{tension reapture} \\ " \quad \text{reapture} + " \quad \text{yielding} \end{array} \right\}$$

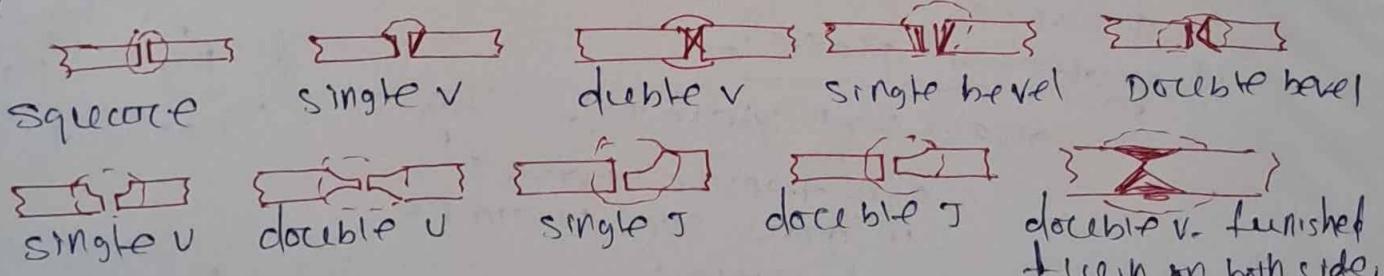
$$= \frac{0.9f_{u,e}A_{vn}}{\sqrt{3}r_{mi}} + \frac{f_y A_{tg}}{r_{mo}}$$

$$\frac{f_y A_{vg}}{\sqrt{3}r_{mo}} + \frac{0.9f_{u,e}A_{vn}}{r_{mi}}$$

- It occurs in joints made with high strength bolts, whence few bolts are required for making the connection.
- When sufficient end distance is not provided, plates may shear out.

3. Welded connections :→

1) Blunt weld



- this type of weld is used when the members are in same plane.

- It is also termed as groove weld.
- It is used to join structural members carrying direct comp. & tension.
- It is used to make tee-joint & butt-joint.

2. Fillet weld !

→ AB or BC → size of weld

BD → throat thickness (t_f)

- this type of weld is used when the members to be connected overlap each other.

- A fillet weld is a weld approximately rectangular cross section joining two surfaces " " as right angles to each other in loop form or tee joint.

- The part of weld which is assumed to be eff. in transferring the stress is called throat.

- It is assumed that fillet weld always offers resistance in the form of shear.

- The dgn. of only is done only for shear in fillet weld.

[t_f = min dimension in fillet weld.]

- The eff. length of fillet weld should not be less than $4 \times$ thickness of weld (s)

Let $t_f = 4 \times$ thickness of weld (s)

- The size of normal fillets shall be taken on the min weld leg size.

- It should not be used if the angle b/w fusion faces is less than 60° & greater than 120° .

- In weld, angle should be b/w 60° to 120° .

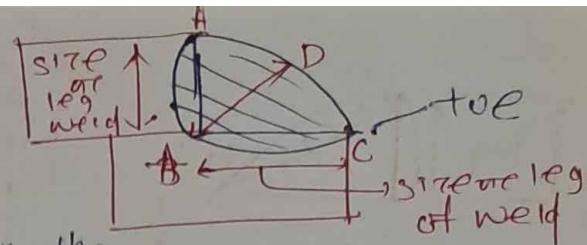
[$t_f = K \times s$ (size of weld)]

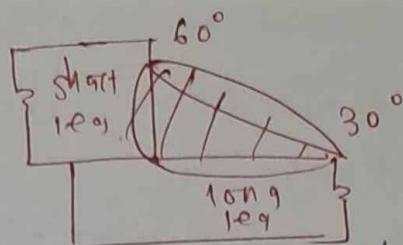
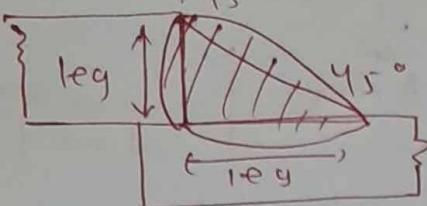
Table-22 value of K for diff' angles b/w fusion faces clause (I.O.S. S-2)

Angle b/w fusion faces	$60^\circ - 90^\circ$	$91^\circ - 100^\circ$	$101^\circ - 106^\circ$	$107^\circ - 113^\circ$	$114^\circ - 120^\circ$
const. K →	0.70	0.65	0.60	0.55	0.50

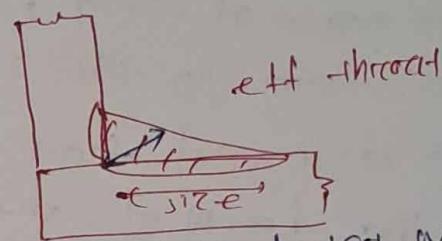
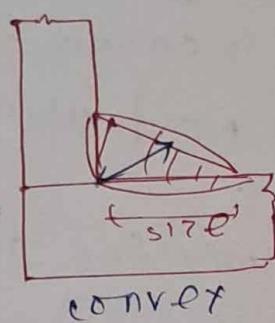
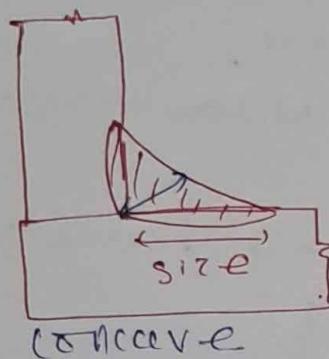
$$\text{Ex!} \rightarrow t_f = (s) \sin 45^\circ$$

$$= 0.75$$





- When the cross section of filled weld is $45^\circ \times 45^\circ$, it's known as a standard filled weld. It is generally used.
- When the cross section of filled weld is $30^\circ \times 60^\circ$ Δ, it's known as special filled weld.
-

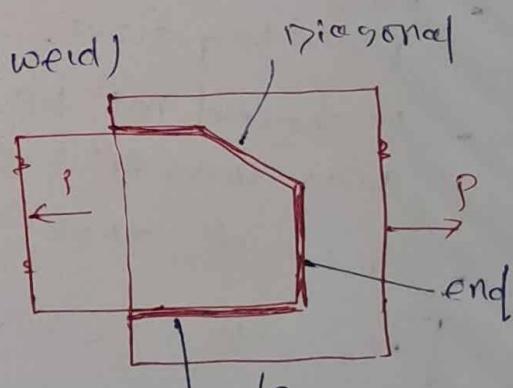


Mitre fillet weld

- A fillet weld is termed as concave fillet weld or convex if " " or mitre depending on the weld face in concave or convex are approximately flat.
- It is termed as normal fillet weld or deep penetration fillet weld depending upon the depth of penetration beyond the root is less than 2.4 mm or more respectively.

i) side filled weld (longitudinal filled weld)

It is stressed in longitudinal shear, i.e., a filled weld, the axis of which is parallel to the direction of the applied loads. It is also



ii) end filled weld (circumferential)

It is stressed in shear i.e., a filled weld, the axis of which is at right angles to the direction of the applied load.

iii) diagonal filled weld

It is a filled weld the axis of which is inclined to the direction of the applied load.

It is placed on the sides or end of the base metal & it is subjected to tens. or comp. & usually bending.

1. size of fillet

Min size of the weld :-

- If the thickness of thicker part :-

Upto 10mm \rightarrow 3 mm

betⁿ 11mm to 20mm \rightarrow 5 mm

21 mm to 32 mm \rightarrow 6 mm

will have to
be taken.

above 32 mm \rightarrow 10 mm
more than 50mm \rightarrow special precaution like preheating
when min size of fillet weld $>$ thickness of thinner part.
then min size of weld = thickness of thinner part.

- It depends on the thickness of thicker plate.

- If thickness is not given, then we assume, $s=3\text{mm}$

Thickness of thicker plate (mm)

0 - 10

11 - 20

21 - 32

> 32

min size of weld (mm)

3

5

6

8 ($\text{if } > 50, \text{ then } 10\text{mm}$)

max size of weld

It also depends upon size of thickness of thinner plate.

case-1

In square edge

max size = thickness of thinner plate - 1.5mm

case-2

After rounded edge.

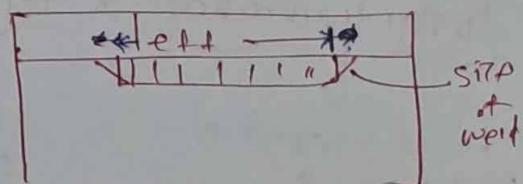
$$= \frac{3}{4} t + (70\% \text{ of the thickness of thinner plate})$$

Eff length of weld

- It depends upon the size of weld.

eff length = Actual length
 $\leftarrow 2 \times \text{size of weld}$

- It should not be less than 4-times the size of weld.

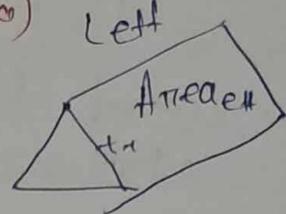


Area of section across at weld (through section)

$$\text{Area eff} = \text{Length} \times t_{\text{eff}}$$

Load carrying capacity of weld or shear strength of weld, $P = f_s \times \text{Length} \times t_{\text{eff}}$

$$= \text{permissible shear stress} \times \text{eff. area of weld}$$



$t_{\text{eff}} \rightarrow$ throat thickness

Length \rightarrow eff. length of weld.

$f_s \rightarrow$ permissible shear stress = 1000 MPa (W.S.M.)

$f_u \rightarrow$ ultimate tensile stress in weld metal.

$$\text{LSM} = \frac{f_u}{\sqrt{3} \times 1.25} \quad (1.25 \text{ for shop weld})$$

$$1.5 \text{ for field "}$$

max pitch, $P = 12t$ or 200 mm \rightarrow comp. zone.

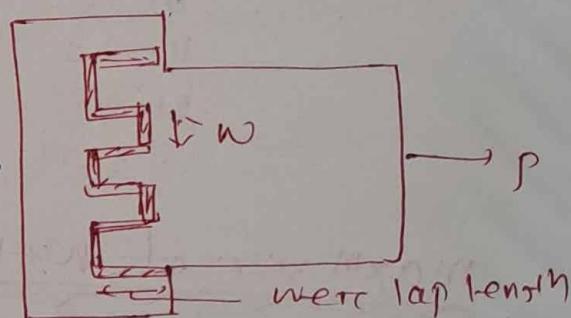
max pitch, $P = 16t$ or 200 mm \rightarrow tens. "

SLOT welding

$w =$ width of slot

$$= \text{max} \{ 25 \text{ mm} \times 3t \}$$

- If overlap length is limited, then the slot welding is done by making slots in the connection plate.



α thickness of plate, $t = 8 \text{ mm}$

$$\text{slot width} = w = 3t = 3 \times 8 = 24 \text{ mm}$$

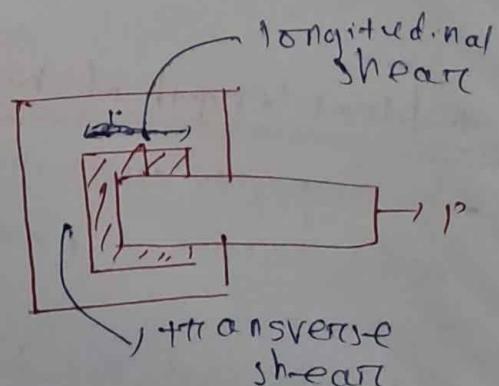
$$w = \text{max} \{ 25 \text{ mm} \times 3t \}$$

$$= \text{max} \{ 25 \text{ mm} \times 24 \text{ mm} \} = 25 \text{ mm. (n)}$$

longitudinal & transverse shear

load & length of weld are same dim.

load & length of weld are ITT to each other



Note

Strength of transverse filled weld is about 30% more than longitudinal fillet weld.

- A fillet welded joint of 6 mm size is shown.

- The welded scored are made at 60° to 90° .

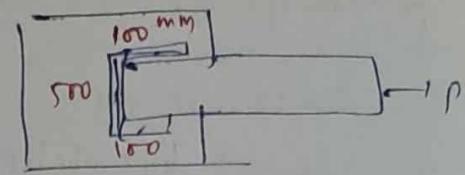
- $F_s = 108 \text{ N/mm}^2$ ~ permissible stress

$$t_f = 0.75 = 0.75 \times 6 = 4.2 \text{ mm}$$

Safe load that can be transmitted by the joint,

$$P = F_s \times t_f \times l_{eff}$$

$$= 108 \times 4.2 \times 250 = 113.4 \text{ kN.}$$



Compression members

- Structural members s.t. axial compression compressive force.
- Their dgn. is governed by strength & buckling.
- Most commonly used comp. member is column.
- Other comp. members are stiffener, truss, frame, etc.

Column

- It is a structural member mainly s.t. comp.
- BM can also exist in this member.
- It is used for comp. of frame, i.e. RCC & steel frame.

Stirrup

- It is a comp. member whose BM is zero because it is used in roof truss as a comp. member.

Truss

- $B.M = 0$ → everywhere.
- It is a struc. in which all the members are either s.t. tension or comp.

Frame

- It is a struc. which is s.t. BM also in addition to tension & comp.

Stanchion

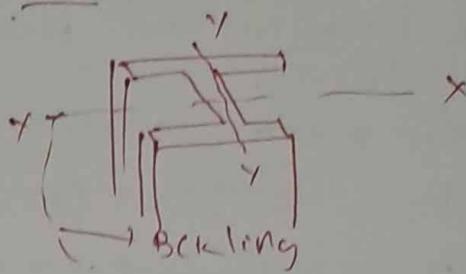
- The vertical comp. member in RCC building is called column while for a steel building it is called stanchion.

Boom

- The principal comp. member in a crane is called boom.

Methods of failure of column:

- 1 - Squeashiny
- 2 - local buckling
- 3 - flexural "
- 4 - tensional "
- 5 - flexural torsional buckling



Squeashiny

When the length is relatively small & the component plate elements are prevented from local buckling, then the column will be able to resist its full strength, i.e., squash load.

$$[\text{squash load} = \text{yield stress} \times \text{Area of cross-sect}]$$

Local buckling

- Failure occurs by buckling of one or more individual plate elements.
- Ex! - flange or web locally prior to overall buckling of column.

Flexural buckling

- In this mode, failure of the member occurs by excessive deflection in the plane of weaker principal axis.
- In the fig., X-X & Y-Y axis's are shown. $I_{xx} > I_{yy}$, so the resistance about Y-Y axis is less as compared to X-X axis. Hence buckling will occur about Y-Y axis.

Torsional buckling

- This type of failure is caused by twisting about longitudinal axis of member.
- It can occur only in doubly symmetrical cross secⁿ with very slender cross sectional elements.

Flexural + torsional buckling

- It is caused by combination of flexural & torsional buckling.
- the member bends & twists simultaneously.
- This type of failure occurs only in unsymmetrical cross sections & singly symmetrical " "

Effective length

- In S.O.M., we use theoretical value & in dgn. we use IS recommended value.
- For flanged columns, above values are ↑ by 5%.
- For bolted " " " " " " " " " " ↑ by 10%.
- eff. length is slightly smaller than the theoretical value to account for the lack of 100% fixity at support.

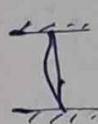
Sl. No. Degree of end restraint of compression member

fig.

theo.
value
of
eff.
length

Recd.
value
of eff.
length

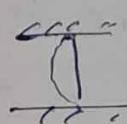
1. Effectively held in position & restrained against rotation in both ends.



0.50l

0.65l

2. Held in position at both ends, against rotation in one end



0.70l

0.80l

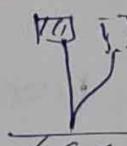
3. Position in both ends but not restrained against rotation



1.00l

1.00l

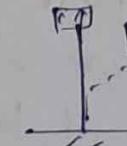
4. Held in position & restricted in one end, & the other " " against rotation but not held in position.



1.00l

1.20l

5. Held in position & restrained in one end, & at the other partially restrained against rotation but not held in position.



1.50l

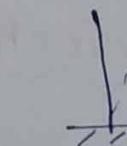
6. Effectively held in position at one end but not restrained against rotation, & at the other end restrained against rotation but not held in position



2.00l

2.00l

7. eff. held in position & restrained against rotation at one end but not held in position nor restrained against rotation at the other end.



2.00l

2.00l

- NOTE
- load capacity of a column depends upon the end cond'n & strongest column is both end fixed.
 - the most efficient cross sectn is resisting compression is thin hollow circular sectn or 'angle box sect'
 - because for a given cross-sectn direct M.O.I is maxm so load carrying capacity is maxm.
 - the most efficient cross sectn in resisting BM is I-sectn because for a given cross sectn eccentric, sectn modulus & plastic modulus are maxm for I-sect.
 - As per IS 800, the permissible axial compressive stress is given by Rankin's merchant formula—

$$\sigma_{ac} = \min \text{ of } \left\{ \frac{0.6 f_y}{\left[\left(F_{ac} \right)^n + (f_y)^n \right]^{1/n}} \right\}$$

$$F_{ac} = \frac{\pi^2 E}{l^2}$$

$n = \text{imperf factor} = 1.4$

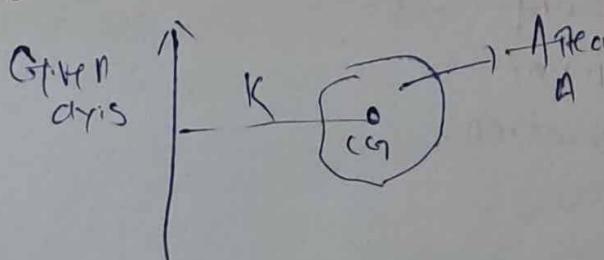
Unsupported length of column—

It is the maxm clear distance betn bottom of the floor level & top of beam.

eff. length of column—

It is length of column betn pts. of zero moment or distance betn pts of contraflexure.

$$\text{Stiffness ratio} = k = \frac{\text{eff. length}}{\text{radius of gyration}} = \frac{l}{r_{min}}$$

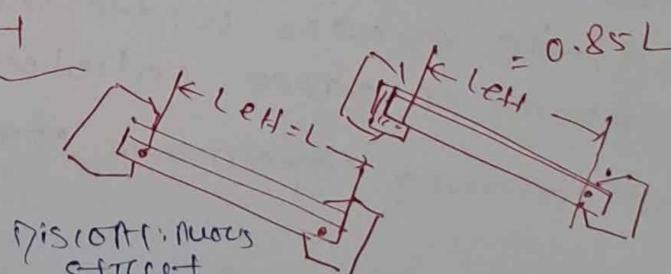
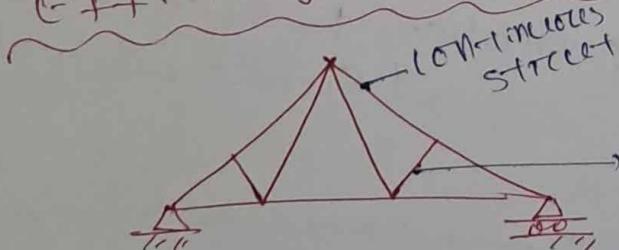


k is the distance such that its square multiplied by area gives moment of inertia about the given axis.

$$k^2 \times A = I \Rightarrow r_{min} = \sqrt{\frac{I}{A}}$$

Sl. No.	Member.	Max value of eff. slenderness ratio $M_{\text{min}} \text{eff.}$ slenderness ratio (kL/r)	Max value of eff. slenderness ratios	
			180	180
1.	A member carrying comp. forces resulting from dead loads & imposed loads	180		
2.	A tension member in which a reversal of direct stress occurs due to loads other than wind & seismic load.	180		
3.	A member st. comp. forces resulting only from combination with wind/earthquake actions provided the deformation of such member doesn't adversely affect the stress in any part of the str.	250		
4.	comp. rigidity of a beam against lateral torsional buckling.	300		
5.	A member normally acting as a tie in a roof truss or a bracing system not considered eff. when st. possible reversal of stress into comp. resulting from the action of wind or earthquake force.)	350		
6.	Members always under tension (other than tie-tensioned members).	400		
	- Tension members, such as bracings, pre-tensioned to avoid sag, need not satisfy the maxm slenderness ratio limits.			

Eff. length of strut



- If a strut span b/w two joint only, it is called as discontinuous strut.
- If a strut span b/w more than two joints then it is called continuous strut.

If rivets are cut at each end, then $L_{eff} = L$

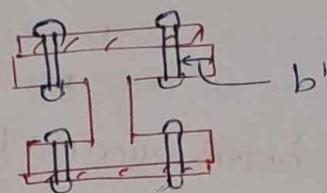
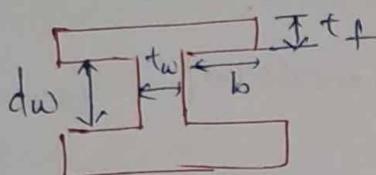
Axial comp. stress $\sigma_{ac} = 0.8$

$\sigma_{ac} \rightarrow$ permissible stress is reduced by 20%.

- If a single angle discontinuous stress is connected by two or more rivets etc. weld, then $L_{eff} = 0.85L$.

$$[\sigma_{ar} = \sigma_{ac}]$$

Local buckling of flange x Web plate of I-section



$b =$ width of flange from face of web.

- Width of overstand is measured from center line of rivet to extreme edge for built up secn.

- To prevent local buckling due to comp. as per IS 800: specify the following cond'ns:-

$$\frac{b}{t_f} \neq 16 \text{ (WSM)}$$

$$\frac{dw}{t_w} \neq 50 \text{ (WSM)}$$

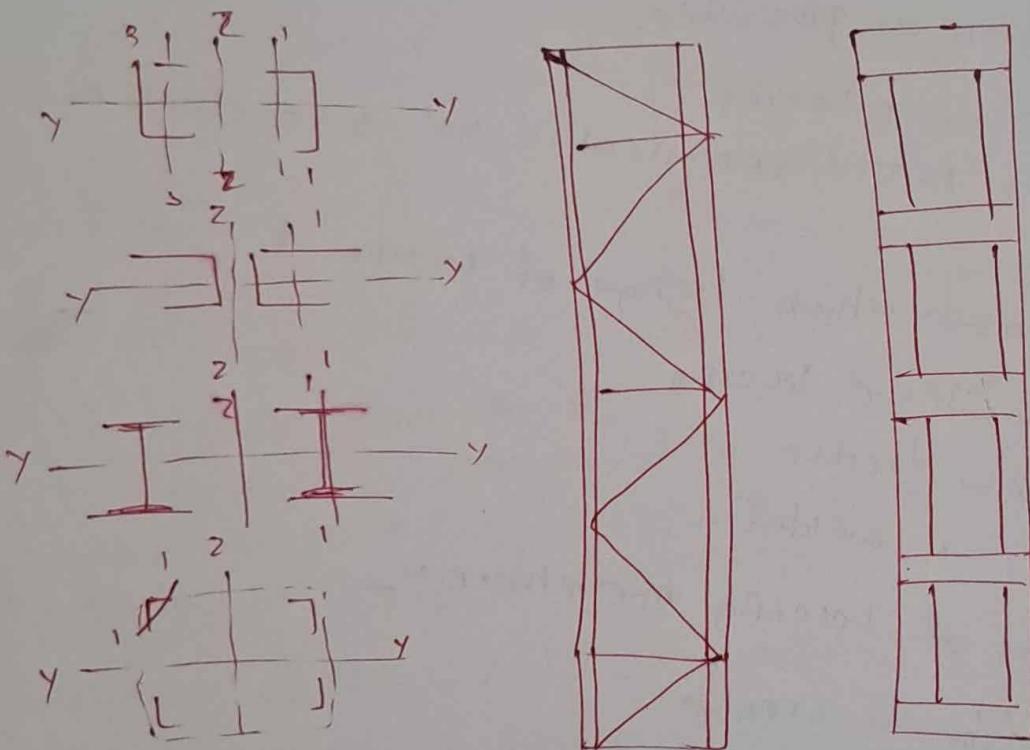
$$\frac{b}{t_f} \neq 8.4 \text{ (LSM)} \rightarrow \text{flange secn}$$

- If the flange x web plate dimensions exceed the above limits, the excess width should be neglected (not considering in actual calculation).
- Load carrying capacity in comp. members, $P = \sigma_{ac} \times A_g$
 $(\sigma_{ac} = 0.6 A_1)$

Built up column

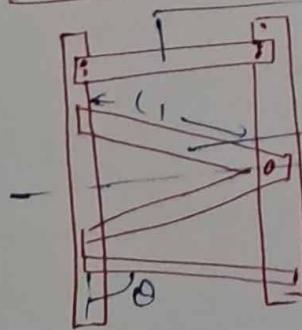
- The size & shape of rolled secn are limited because of limitations of rolling mills, so when rolled secns don't furnish the required sectional area or when a special shape or large radii of gyration are required in two different dirns, built up columns are used.

- Br. Anjana Khamari**
- are widely used in steel construction especially when the eff. lengths are greater & the comp. forces light.
 - they are composed of two or more parallel main components interconnected by lacing or batten plates.
 - the greater the distance b/w the chord axes, the greater is the moment of inertia of the built-up cross section, the \uparrow in stiffness, however is counterbalanced by the \uparrow wt. & cost of the connection of members.
 - it should be noted that built-up columns (especially bolted built-up columns) are more flexible than solid columns w/in the same mol.



Lacings

Tie plate or Batten plate



Lacing

Transverse S.F

$$V = 2.5\% \text{ of column load}$$

- Lacing is a system of connecting elements in built up column.
- If make the components of column act as a single unit.

- If the components of column are each very close to each other, then thick rivets are used to make them act as a single unit.
- If the spacing of component is more than the rivets are useless & so we use lacing or batten.

Inclined members - lacing

- Batten

Horizontal "

- It is idealised as truss elements, i.e., the are st. either to tension or comp.

- $B.M = 0 \rightarrow$ in lacing.

To ensure that $B.M = 0$, provide only one rivet at each end as force is possible.

- $\max^m \delta = 145 \rightarrow$ in lacing

Ankle of lacing w.r.t vertical is 40° to 70° (welding 60° to 90°).

- If α decreases then length of lacing \uparrow .

- $L_{eff} = L_1 \rightarrow$ single lacing

$$= 0.7L_1 \rightarrow \text{double "}$$

$$= 0.7L_1 \rightarrow \text{welded ..}$$

- Min thickness of lacing member :-

$$t_{min} = \frac{l_1}{40} \rightarrow \text{single}$$

$$= \frac{l_1}{60} \rightarrow \text{double.}$$

- min width :-

nominal dia of rivet		
16 mm		50 mm
18 mm		55 mm
20 mm		60 mm
22 mm		65 mm

- It depends upon the nominal dia. of rivet.

- In case of welding, width of lacing bar is 50mm

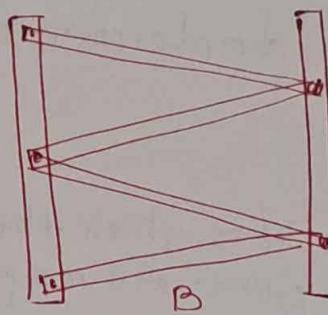
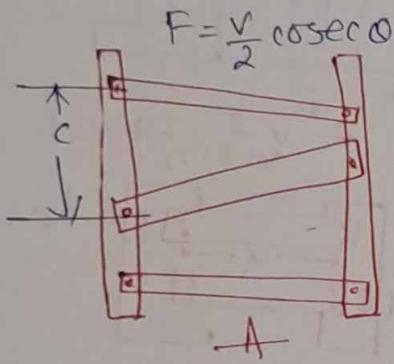
Er. Anjana Khamari even buckling of column component b/w facing connection! —

↓ component + 50
↓ 0.7 ↓ column

For back rivets: —

↓ component + 40
↓ 0.6 ↓ column

- At the end of facing system, at top & bottom, tie plates are provided (tie plate is called batten plate).
- These batten plate prevent distortion of built up columns.



$$F = \frac{2V}{N} \operatorname{cot} \theta$$
$$f = V \operatorname{cot} \theta$$

- Arrangement in 'A' is better than 'B', because if one tie plate fails, spacing of facing members doesn't change in 'A' while in 'B', spacing will be doubled. Hence there will be possibility of buckling of connection in 'B'.

Stress forces in facing members: →

- Facing system is designed to resist a transverse s.f. of $V = 2.5\% \text{ of column load}$.
- The transverse s.f. V is shared by facing system both ends equally, so the transverse s.f. on each facing here is $\frac{V}{2}$.

* 2 denotes no. of parallel plates.

* $f = \frac{V}{2 \sin \theta}$ → single → two parallel force system force in each facing bar

* $F = \frac{V}{4 \sin \theta}$ → double

Battens

- It behave like very small beam members & s.t. BM.
- the eff. length of beam-reinforced column should be \uparrow by 10%.
- minⁿ no. of battens provided = 4
- provided batten on opposite tees such that one should be the mirror image of other.
- eff. slenderness ratio,

$$\lambda = 1.10 \frac{L_0}{c} \uparrow \text{by } 10\% \text{ in battens}$$

$L_0 \rightarrow \text{max}^m \text{ actual slenderness ratio}$

- eff. depth :-

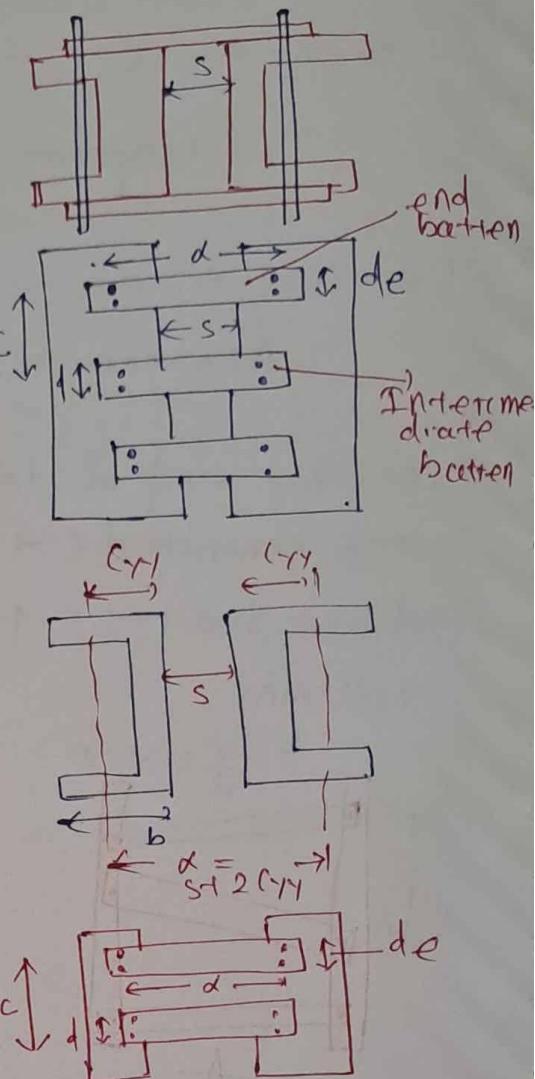
- It should not be less than the distance between centroid component members. $de + \alpha$
- It should not be less than twice the width of one component in plane of batten (b).
 $de + 2b$.
- thickness of batten (t) :- $t \geq \frac{\alpha}{50}$
- To prevent local buckling of individual component between the battens, following condns are satisfied ! -

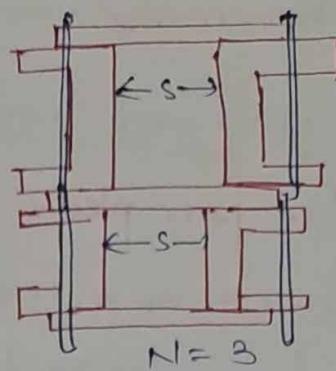
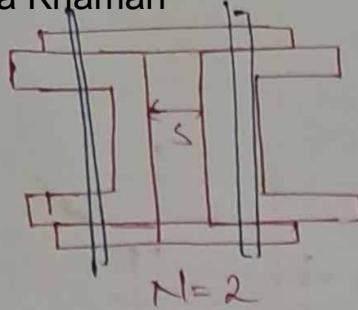
$$\cdot \frac{c}{f_{CY}} < 50$$

$$\cdot \frac{c}{f_{CY}} < 0.7 \text{ d}_{\text{column}}$$

- For Intermediate batten,
 $de \geq \frac{3}{4} \alpha$
 $de \geq 2b$

- For end batten,
 $de \geq \alpha$
 $de \geq 2b$

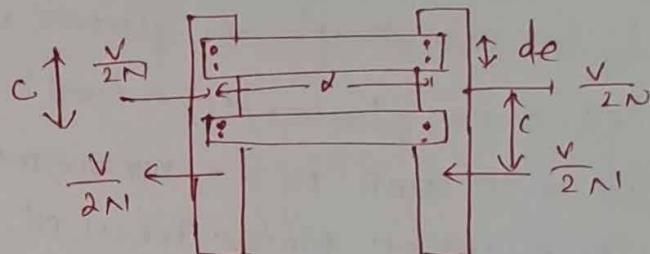




→ Transverse s.f. V is sheared by parallel planes (N) equally
i.e. transverse s.f. each batter = $\frac{V}{N}$

$$N = \text{No. of parallel planes}$$

- Batters should be designed to carry BM & SF arising from the transverse s.f., which is 2.5% of total axial load on comp. members.



- the transverse s.f. is equally divided in all the parallel planes N in which there are shear resisting elements such as batters or continuous plates batters.
- Batters should be able to resist the longitudinal shear & moments arising from transverse shear V .

$$\text{Longitudinal shear} (V_L) = \frac{Vc}{N\alpha}$$

V → transverse s.f. → 2.5% of P

N → no. of parallel planes of batters.

$$\text{Longitudinal moment} (M) = \frac{Vc}{2N}$$

Column Splicing

- Splicing of column is done to ↑ the length of column.
- the most suitable location for column splices is at a suitable location of $\frac{H}{3}$ to $\frac{H}{4}$ from the top & bottom level floors.
- When the column end are machined then it is assumed that 50% of load is transferred by direct bearing action & remaining 50% of the load is transferred through splice & its connection.

$\frac{P}{2}$ → splice end connection

$\frac{P}{4}$ → each splice plate

- If a column is s.t. do a comp.

load P , the $\frac{P}{2}$ is transferred

by beccring connexion & remaining

$\frac{P}{2}$ is taken by splicing plate,

$\frac{P}{4}$ by each splicing plate (since 2

splicing plates are used).

- If a column is s.t. moment M also,

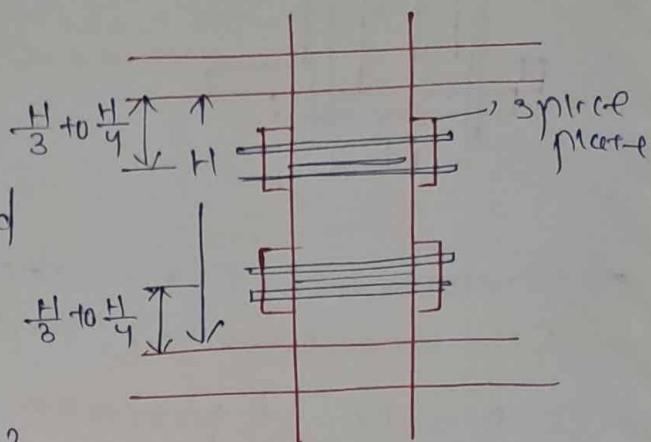
then splice plate must also resist

additional force of $\frac{M}{H}$, so

max^m force in splice plate's

max^m load for each splice

$$\text{plate} = \frac{P}{4} + \frac{M}{H}$$



NOTE

If the column ends are not smooth, for complete beccring, entire load is assumed to be transferred to the bottom column through splice plate & connection only.

Hence max^m force in each splice plate

When column ends are not smooth.

$\frac{P}{2}$ → Each splice plate

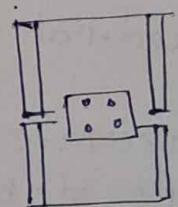
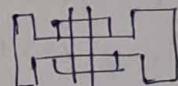
$$\text{max load for } " " " = \frac{P}{2} + \frac{M}{H}$$

If s.f is also acting at a column splice, a web splice

must be done, both side of the web as shown.

The rivets in web splice are s.t. double shear & bearing

but rivets in flange splice are s.t. single shear & beccring.

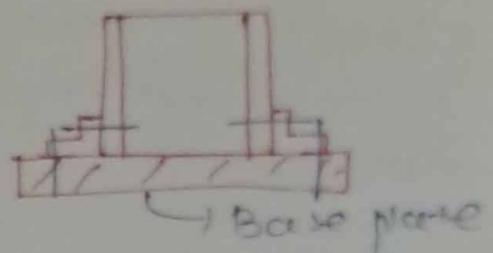


→

Slab Base

Column base

- It is a base plate used to reduce the bearing pressure on the concrete footing.
- It distributes the load to the concrete footing, preventing the punching shear of footing.
- If the column load is more less, slab base is used.
- If the " " " " " heavy/heavy, then gusseted base is used.
- If the soil is weak, grillage foundation is used.



Slab base

- permissible tensile stresses of bolt used in column base is 120 MPa.
- In slab base, base plates & clear angle are used.
- If column load is axial, then thickness of base plate is given by -

$$t = \sqrt{\frac{3W}{6\sigma_s}} \left(d^2 - \frac{b^2}{4} \right) \rightarrow WSM$$

$$t = \sqrt{\frac{2.5W}{6\sigma_s}} \left(a^2 - 0.33b^2 \right) \rightarrow LSM$$

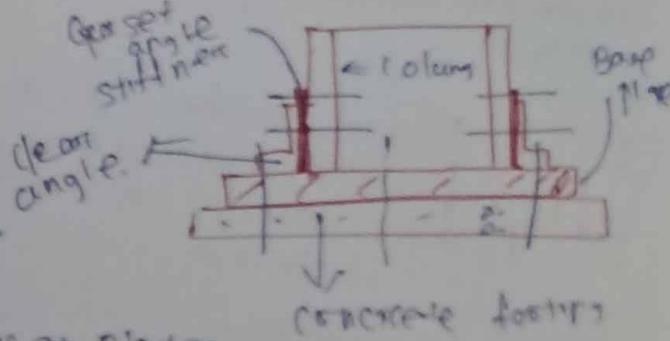
w → upwarded pressure on base plate in N/mm^2

a, b → greater & smaller projection of base plate beyond column edge.

σ_s → permissible bearing comp. stress in base plate.

Gusset Base

- Adopted when the load is large.
- Axial load accompanied by BM.
- Having eccentric loadings.
- Area can be ↑ by adding gusset plates.

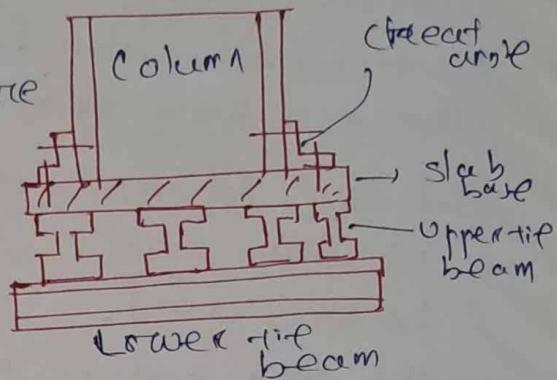


Er. Anjana Khamari

- Critical section for BM is cut more of gusset plate, cortex & kernel: — It is the small portion at cross section within which load is applied, tension will not be developed.

Gullage found!

- Adopted when loads on columns are extremely heavy.
- the bending capacity of soil for the area of gusset / slab is not enough.
- distribution area is very large.



Beams

→ It is a structural member s.t. transverse load.

flexural formula: — $\frac{M}{I} = \frac{\sigma}{Y} = \frac{E}{R}$

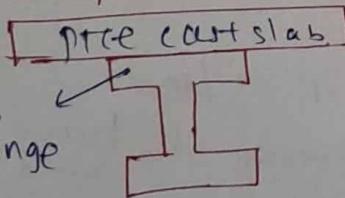
$R \rightarrow$ Radius of curvature

$\frac{1}{R} \rightarrow$ curvature.

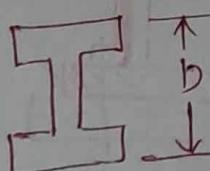
Moment is directly proportional to curvature.

Moment $\propto \frac{1}{R}$.

Laterally unsupported beam



- If the comp. flange of beam is not restrained against lateral moment, then it is called as L.U.B or.

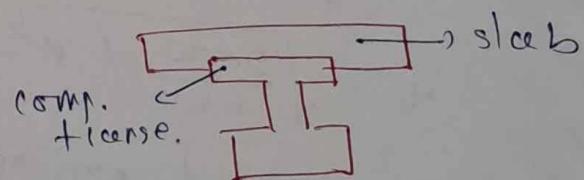


→ In the dgn. of beam

We assume that the depth of web is resisting shear is taken as overall depth of the beam.

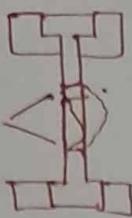
$$[T_{ra} \text{ calculate} = \frac{V}{Dtw}]$$

Laterally supported beam



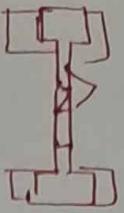
- If the comp. flange of beam is restrained against lateral moment, then it is called as laterally supported beam or laterally restrained beam.

We assume that the depth of web is resisting shear is taken as overall depth of the beam.

web buckling

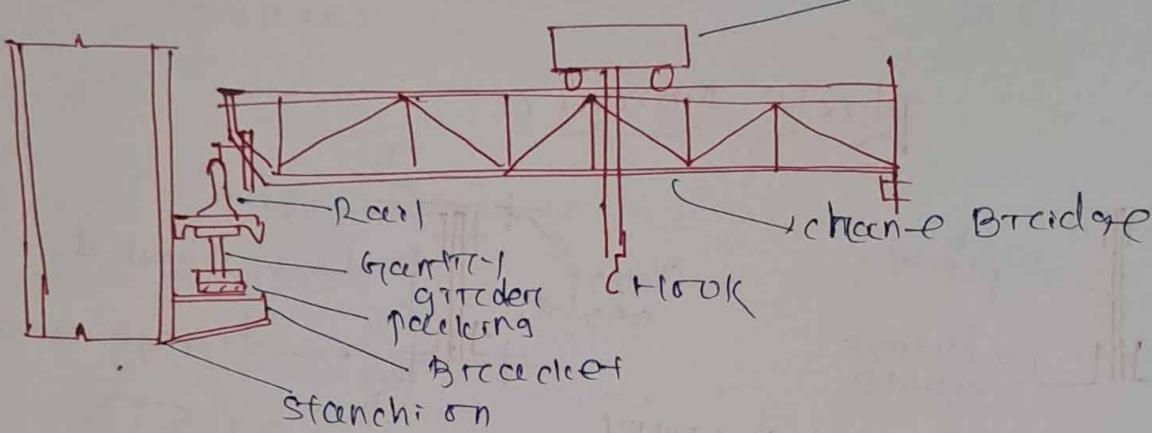
H occurs due to diagonal comp. in web / concentrated load which is produced due to S.F. in web.

- H occurs near toe of fillet weld.

web crippling / local buckling of web

→ web near the junction of the stress cone tends to fold over the flange called web crippling.

- Developed due to large amount of bending stress.
- Stress conc. occurs at the junction of web & flange.

Gantry Girders

It is subjected to:

- i) Gravity loads (i.e. DL + LL + wt. of eccentricus + wt. of trolley, etc.).

ii) Lateral load (due to starting or stopping of trolley)

iii) Longitudinal " (" " " " of crane)

- these three loads are mutually perpendicular to each other.
- Horizontal & vertical loads are applied simultaneously.
- allowable stress in gantry girder will be $\frac{1}{3}$ of by 10%.

Additional load due to impact.

Type of loading

Impact allowanceVertical load

1. E.O.C

\rightarrow 25% max static wheel load

2. M.O.C

\rightarrow 10% " " " "

Horizontal force transverse to rail

1. E.O.C

\rightarrow 10% wt. of trolley & wt. lifted

2. M.O.C

\rightarrow 5% " " " "

Horizontal force along the rail \rightarrow 5% of static wheel load.

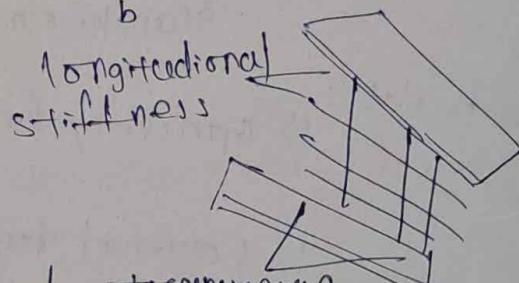
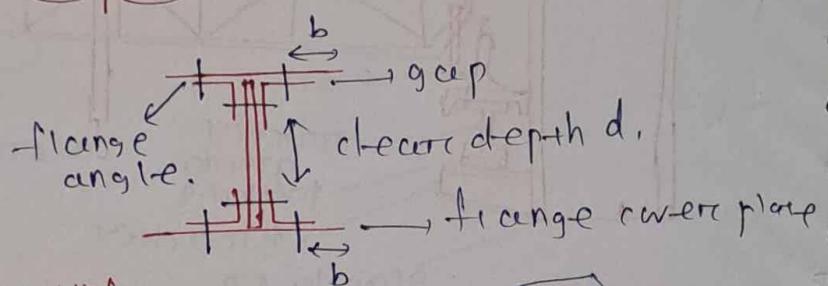
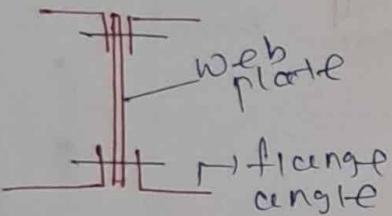
- These crane booms originally designed to carry heavy loads from place to place at the construction sites. → maxm permissible def'n

$$1. \text{ For } \delta = \frac{\text{Span}}{500} \rightarrow \text{for manually operated crane.}$$

$$2. \delta = \frac{\text{Span}}{750} \rightarrow \text{electrically operated crane capacity up to 50 T or 500 kN}$$

$$3. \delta = \frac{\text{Span}}{1000} \rightarrow \text{" more than capacity 50 + 50 kN}$$

Plate Girders



- A plate girder is used as a flexural member whose cross secn is composed of plate elements, flange plate, angles & web equivalent.
- If built up beam can't withstand applied load then plate girder is used.
- It consists of flange plate, flange angle & web plate.
- It consists of flange plate, flange angle & web equivalent.
- Web equivalent is the web area embedded between two flange angle.
- In comp. zone flange, web equivalent is taken as $\frac{\text{effect of web}}{6}$
- OR $\frac{a_w}{6}$.

Tension Flange

- It consists of flange plate, angle & web equivalent.

- In tension zone, web equivalent is taken as

$$\frac{a_w}{8}$$

- There is assumed that entities S.F is taken by web plate & B.M is taken by flange so to ensure that web takes only S.F, gap of s_m will be maintained b/w flange plates & web plate so that direct bearing eccentricity b/w flange plate & web plate is avoided.

- The load is transferred from flange plate to web plate through flange angles only.

- Width of overstand in comp. flanges $\rightarrow \frac{b + 16t_f}{b + 256t_f}$

" tension " $\rightarrow b + 20t_f$

- Economical depth of web plate (which is corresponding to min wt. bearing min cost).

$$d = 1.1 \sqrt{\frac{M}{6bc \times t_w}}$$

- Self wt. of plate girder is assumed as:

$$w = \frac{w}{300} \text{ kN/m} \rightarrow wsm$$

$$= \frac{1.5 w}{300} \text{ kN/m} \rightarrow lsm = \frac{w}{200} \text{ kN/m}$$

- If $\frac{d_i}{t_w} < 85$, web buckling due to shear will not happen, so stiffeners are not provided. The web will be unstiffened.

- If $\frac{d_i}{t_w} > 85$, vertical " " provided to prevent buckling of web due to diagonal comp. which is developed due to S.F.

- If $\frac{d_i}{t_w} > 250$, horizontal stiffeners are provided above NA as they prevent buckling web due to bending comp stress.

- If $\frac{d_i}{t_w} > 250$, then additional horizontal stiffeners are provided at N.A.

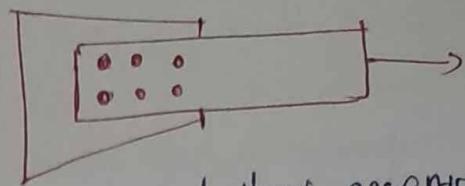
- If $\frac{d_i}{t_w} > 400$, then section must be redesigned.

- After providing all the stiffeners, lesser clear dimension of web panel should not exceed $180t_w$.

- If greater clear dimension of web panel $> 270t_w$.

Tension members (tie)

- A structural member s.t. axial tension is called tension member or tie.
- the members & connections are so arranged that eccentricity in the connection & bending stress are not developed.



Types of failure

1. Gross secⁿ yielding:-
considerable deformation of the member in longitudinal direction may take place before it fractures, making the str. unserviceable. Hence we must also consider yielding on gross-sectⁿ.

2. Net secⁿ rupture:-
the fracture of the member occurs when the net cross-sect of the member reaches ultimate stress.

3. Block shear failure:-
A segment of block of material at the end of member shears out due to the possible use of high bearing strength of steel & high strength bolts providing in smaller connection length.

Dgn. strength of TM:-

1. Gross secⁿ yielding:-
 $T_{dg} = \frac{f_y}{\gamma_m} \cdot A_g$ → Gross sectional area
dgn. strength.

- When a TM is st. tensile force although the net cross-sect yields 1st, the deformation within the length of connection will be smaller than the 1st in the remainder of TM. It is because the net action exist within the small length of member, most of the length of member will have an un-reduced cross-sectⁿ, so attainment of yield stress on gross area will result in larger total elongation.

2. Net secⁿ rupture (fracture):-
Ultimate strength of material

$$T_{dn} = \frac{0.9 f_u}{\gamma_m} \cdot A_n \rightarrow \text{etd. net area of cb}$$

dgn. strength in rupture. $\rightarrow 1.25$

- For plates:-

- For shear yield & tension fracture:-

$$T_{db1} = \frac{A_y A_{vg}}{\sqrt{3} R_{mo}} + \frac{0.9 A_t A_{en}}{R_m}$$

- For tension yield & shear fracture:-

$$T_{db2} = \frac{A_y A_{vg}}{\sqrt{R_{mo}}} + \frac{0.9 A_t A_{en}}{\sqrt{3} R_m}$$

Where,

$A_{vg} \rightarrow$ min^m gross area in shear along the line of force

$A_{en} \rightarrow$ " net " " " " " "

$A_{vg} \rightarrow$ " gross " in tension

$A_{en} \rightarrow$ " net " " "

Slenderness ratio in TM:-

- It is the ratio of its unsupported length 'L' to its least radius of gyration.

- Max^m slenderness ratio for tension members is given as:-

* A TM in which reversal of direct stress due to loads other than wind or seismic force occur. $\rightarrow 180$

* A member normally acting as a tie in roof truss or a bracing system s.t. possible reversal of stresses resulting from the action of wind & earthquake forces. $\rightarrow 350$

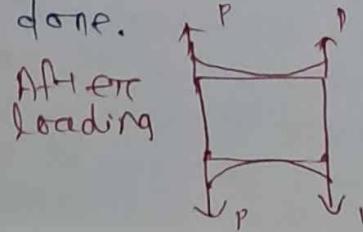
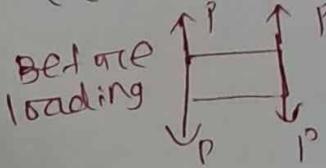
* Members always under tension (other than pre-tensioned members) $\rightarrow 400$

SHEAR LEG

- Non uniform stressing of member due to tension is called shear leg.

- It reduce the efficiency of TM that are not connected to gusset plate.

- For reducing shear leg, lengthening of connections & reduction in efficiency is done.



Increase in length
reducing the
efficiency.

LONG JOINT (LJ)

L = overclapping length.

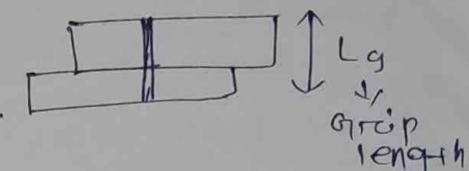
If $L > 15\phi$ or $L > 150t_e$ then it is called long joint.

- It is assumed that applied load is shared by all the rivets, but in LJ, outer rivets takes more load than the inner. So failure of rivets in long joints is sequential, beginning with those at the ends & progressing towards centre, this type of failure is termed as 'unbursting'.

- If length of joint is more then efficiency of the TM would be less.

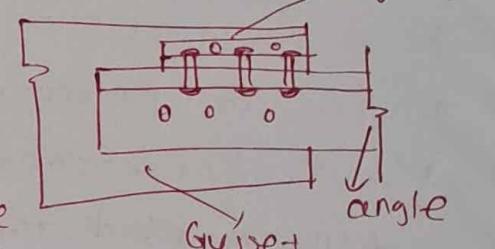
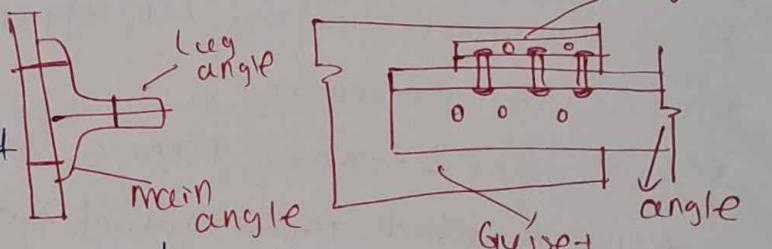
$$L_g = 5\phi \text{ (LSM)}$$

$$L_g = 8\phi \text{ (NSM)}$$



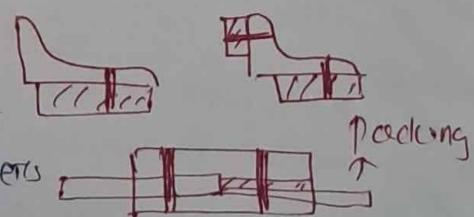
- If L_g increases then efficiency of joints decreases due to additional bending stress developing in rivets.

LUG ANGLES



- It is small piece of angle used to connect the outer end leg of the structural members to the gusset plate.
 - The purpose of lug angle is to reduce the length of connection to gusset plate & reduce the shear leg effect.
- * shear leg effect is reduced by increasing the length of connection & by providing lug angles.

- If lug angle are used, the efficiency of TM increases.
- If length is increased, then shear leg effect is decreased but efficiency is also decreased. If lug angle is used then efficiency is increased & shear leg is reduced.



SPLICES

- They are used to joint two rods when a joint is to be provided, i.e., these place the members at the joint where it is cut.
- When a splice occurs in an angle, channel, tee or joint sec", the force is received from the member through the connection on one side of joint & is transferred to the splice cover plate.
- The force is then carried through these covers across the joint & is transferred to other portion of member through the connections.

Local carrying capacity of tension members

$P_t \rightarrow$ safe local carrying capacity

$$P_t = G_{ot} A_{net} (\text{W.S.M})$$

whence,

$G_{ot} \rightarrow$ permissible axial tensile stress = 0.6 f_y

$A_{net} \rightarrow$ Net effective ch/c area.

$$P_t = \min \left\{ A_g \frac{f_y}{1.10} \mid A_{net} \frac{0.9 f_u}{1.25} \right\}$$

- To prevent fracture:-

$$A_{eff} = 0.9 A_{net}$$

$$P_t = A_{eff} \frac{f_u}{1.25}$$

For plate:-

calculate of A_{net}

i) chain riveting, $A_{net} = (B - 3d)t$

ii) diamond " , $A_{net} = (B - d)t$

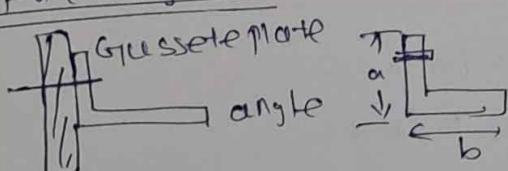
iii) staggered " , $A_{net} = (B - n_1 d + \frac{\pi r_1^2}{4g_1} + \frac{\pi r_2^2}{4g_2})t$

$n_1 \rightarrow$ no. of rivets along circumferential secn

$d \rightarrow$ gross dia. or hole dia.

$r_1, \& r_2 \rightarrow$ staggered pitch

" gauge.

For angles

$$A_1 = (a - d - \frac{t}{2})t$$

$$A_2 = (b - \frac{t}{2})t$$

- calculation of A_{net}

- for angle:- $A_{net} = (A_1 + K A_2)$

$$K = \frac{3A_1}{3A_1 + A_2}$$

L, shear leg effect

$A_1 \rightarrow$ net area of connected leg

= gross area of " " -
area of rivet hole

$A_2 =$ gross area of unconnected leg

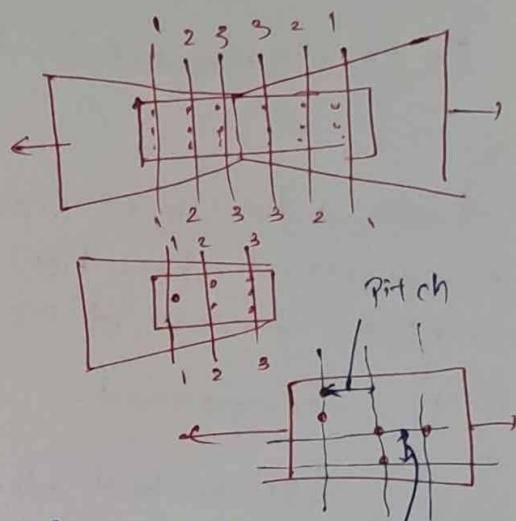
- If two angles are placed back to back outstand leg.

& connected to both sides of gusset plate.

$$K=1 \rightarrow \text{then } A_{net} = (A_1 + A_2)$$

- It is most efficient way of connecting, then load carrying capacity is max.

- If the two angles don't have rivet then each angle behaves independently hence, $K = \frac{3A_1}{3A_1 + A_2}$



1. To find A_{net} required?

$$A_{net} \text{ required} = \frac{P}{6\sigma_t}$$

2. ↑ A_{net} by 40-10 50% to get A_g required when riveting is done.

3. ↑ A_{net} by 20% to get A_g required when welding is done.

4. Select a suitable sec'n & find the no. of rivets required.

5. If A_g provided > A_g required, so dyn. is safe.

Q
check whether single angle of T11 in welded steel is required that has area 475 mm^2 to be dyned for axial tension force of 501 N, $\sigma_{ut} = 150 \text{ MPa}$.

$$\rightarrow A_{required} = \frac{P}{6\sigma_t} = \frac{50000 \text{ N}}{150 \text{ N/mm}^2} = 333.33 \text{ mm}^2$$

$A_{provided} = 475 \text{ mm}^2 > 333.33 \text{ mm}^2$ (dyn. safe)

As per IS 800

- In case of single angles in tension connected by one leg only, the net eff. area = $a + \frac{b}{16(0.2)\frac{b}{a}}$
- eff. area of plate girders, in tension = $A_f + \frac{A_w}{8}$
in comp. = $A_f + A_w$

As per IS 800 for mild steel:

Proportional limit $\rightarrow 190-220 \text{ N/mm}^2$

Yield strength $\rightarrow 230-250 \text{ N/mm}^2$

Ultimate " $\rightarrow 410-450 \text{ N/mm}^2$

Fatigue " $\rightarrow 250-300 \text{ N/mm}^2$

Elongation of fracture $\rightarrow 23-35 \text{ %}$

Bearing stress $\rightarrow 0.75 \text{ f}_y$

NOTE

- Vertical stiffeners are provided to prevent shear buckling of web.
- Horizontal stiffeners are .. to avoid comp. buckling.

Vertical stiffeners:

- These are not designed as column.
- Min spacing is $\frac{d_i}{3} = 0.33d$.
- max^m " = 1.5d.

End bearing stiffeners:

They are designed as imaginary column with both end are fixed whose eff. length = $0.7l$.

DESIGN OF STEEL STRUCTURE

Er.Anjana Khamari

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Module I

- Introduction, advantages/disadvantages of steel, rolled steel section, various type of loads, design philosophy.
- Limit state design method, limit state of strength and serviceability, Probabilistic basis for design, Riveted, bolted and pinned connections.
- Welded connections - assumptions, types, design of fillet welds, intermittent fillet weld, plug and slot weld, failure of welded joints vs bolted and riveted joints.

Module II

Tension members, types, net cross-sectional areas, types of failure, slenderness ratio, design of tension members, gusset plate.

Module III

- Compression members, effective length, slenderness ratio, types of cross section, classification of cross section.
- Design of axially loaded compression members, flanging, battering, design of column base and foundation bolts.

Module IV

Design of beams, types of Cf, lateral stability of beam, lateral torsional buckling, bending and shear strength, web buckling and web crippling, deflection, design procedure.

Module V

Plate girders - various elements and design of components, eccentric and moment connections, roof trusses.

Book
Limit state design of steel structures by SK Duggal

IS 800:2007

I slab

the below note for slab thickness, reinforcement, reinforcement
protection, slab thickness, slab reinforcement, reinforcement
protection for shear, bottom girder end and the
bottom girder end, between deck of slab thickness,
slab thickness, reinforcement - reinforcement
bottom for slab, deck thickness and slab thickness
bottom for slab, deck thickness and slab thickness

II slab

note for slab, deck thickness and slab thickness
and thickness, reinforcement for slab, reinforcement
bottom for slab, deck thickness and slab thickness

III slab

note for slab, reinforcement, reinforcement
protection and reinforcement for slab thickness, reinforcement
bottom for slab, reinforcement for slab thickness
and reinforcement for slab thickness

IV slab

note for slab, reinforcement for slab thickness, reinforcement
for slab thickness and reinforcement for slab thickness, reinforcement
bottom for slab, reinforcement for slab thickness
and reinforcement for slab thickness

V slab

note for slab, reinforcement for slab thickness, reinforcement
for slab thickness and reinforcement for slab thickness, reinforcement
bottom for slab, reinforcement for slab thickness
and reinforcement for slab thickness

Ingredients of Cement

- 1) Lime
- 2) Silica - 20%
- 3) Alumina
- 4) Gypsum
- 5) Iron Oxide
- 6) Magnesia
- 7) Sulphur Trioxide
- 8) Soda and potash

Introduction

- A steel structures is an assemblage of a group of members expected to sustain their share of applied forces and to transfer them safely to the ground.
- Depending upon the orientation of the member in the structure and its structural use, the member is subjected to forces either axial, bending or torsion or a combination thereof.
- Axial load can be either tensile or compressive and accordingly the members are called tension members or compression members.

Advantages of Steel

- 1) Steel members have high strength per unit weight.
- 2) Steel being a ductile material does not fail suddenly but gives visible evidence of impending failure by large deflections.
- 3) Structural steels are tough i.e. they have both strength and ductile.
- 4) Being light steel members can be conveniently handled and transported.
- 5) Properly maintained steel structures have a long life.
- 6) The properties of steel mostly do not change with time.
- 7) Additions and alterations can be made easily to steel structure.
- 8) They can be erected as a faster rate.

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Steel has the highest scrap value amongst all building materials.
Steel is the ultimate recyclable material.

Disadvantages of Steel

- 1) Steel structures when placed in exposed conditions are subjected to corrosion.
- 2) The use of weathering steel however in suitable applications may eliminate the requirement of frequent painting.
- 3) Steel structures need fireproof treatment which increases cost.
- 4) Fatigue of steel is one of the major drawbacks. It involves a reduction in the strength when steel is subjected to large number of stress reversals and even to a large number of variations of tensile stress.
- 5) At the place of stress concentration in the steel section under certain conditions the steel may lose its ductility.

8/1/25

Tension Member

The axial load can be tensile members is called tension members.

Ex → Tie

Compression Member

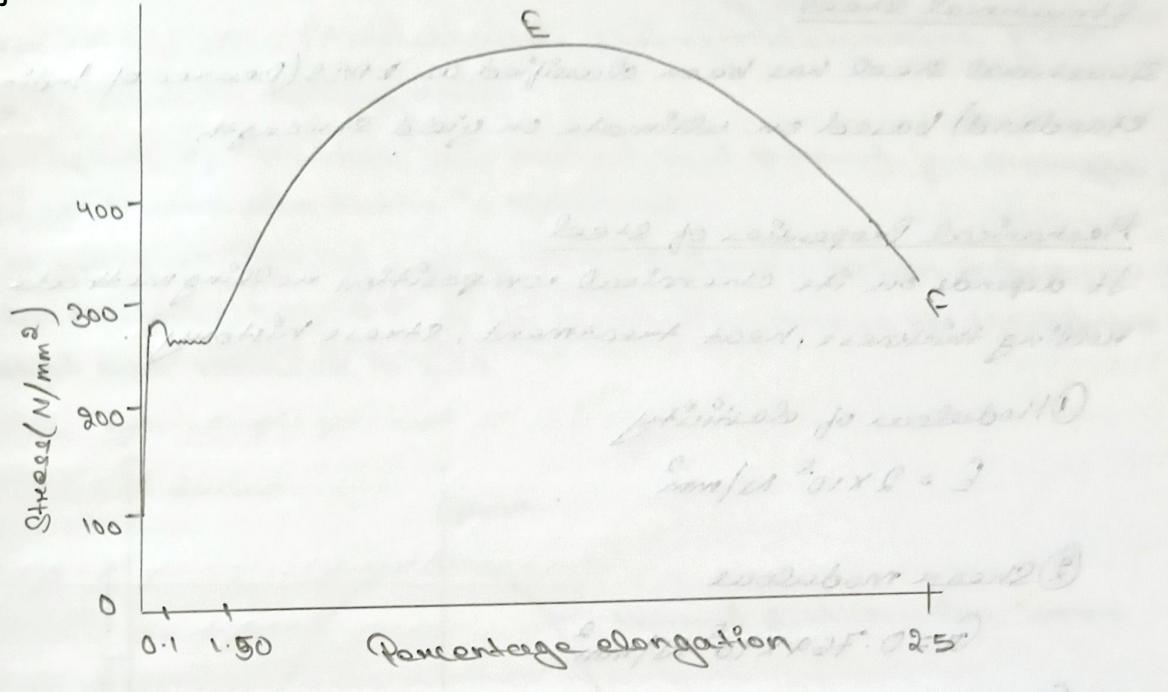
The axial load may be compressive member is called compression member.

Ex → Steel

Column

Design of Structural elements

The position of elements i.e. beam, column, steeple, purlin etc are used to planning the architecture design of building.



(a) Stress strain curve of mild steel
0.02 square mm test dia.

Properties of Steel

- 1) Carbon
- 2) Sulphur
- 3) Phosphorus
- 4) Manganese
- 5) Silicon

(b) Strength properties

most strongest material - 270
percentage 100%

It is achieved - need to add sol. metal of tungsten & other
heat sink. which should not be enough owing
to low number of brittle heat treated materials at
higher temperatures

17/1/25
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Structural Steel

Structural steel has been classified as IS 2081 (Bureau of Indian Standard) based on ultimate or yield strength.

Mechanical Properties of Steel

It depends on its chemical composition, rolling methods, rolling thickness, heat treatment, stress history.

① Modulus of elasticity

$$E = 2 \times 10^5 \text{ N/mm}^2$$

② Shear modulus

$$G = 0.769 \times 10^5 \text{ N/mm}^2$$

③ Poisson's ratio (ν)

a) Elastic range = 0.3

b) Plastic range = 0.5

④ Coefficient of thermal expansion

$$12 \times 10^{-6}/^\circ\text{C}$$

27/1/25

Ultimate Strength (UTS)

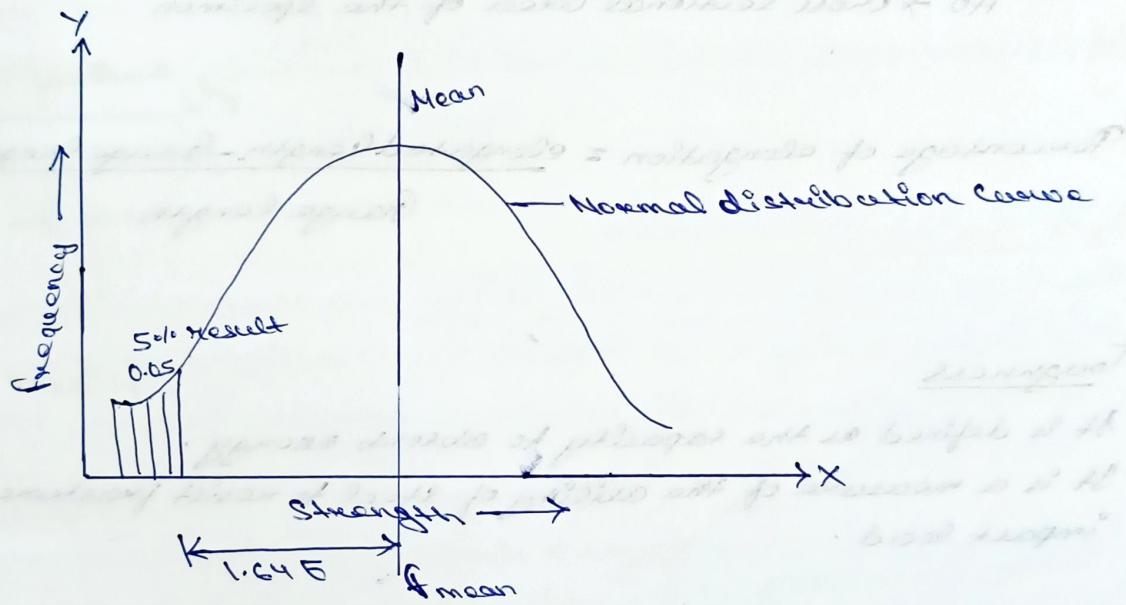
$$\text{UTS} = \frac{\text{Ultimate tensile load}}{\text{Cross sectional area}}$$

- If it is subjected to tension, the area of cross-section of the specimen decreases and the ultimate strength stress would be ultimate tensile load divided by reduced area of cross section.

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of steel is

- As per IS 200, the characteristic strength is determined from test of steel in rolling mill.
- If a number of specimen are tested and plotted for strength, a normal distribution curve is obtained.
- The characteristic strength is the minimum value below which not more than 5% of corresponding stress of specimens tested are expected to fail.



$$\text{Characteristic Strength, } f_{ck} = f_{mean} - 1.645 \sigma$$

where,

σ = Standard deviation

$$\sigma = \sqrt{\frac{\sum (f_{mean} - f)^2}{(n-1) 0.5}}$$

where,

n = no. of specimens

Ductility

- It is another fundamental property of steel.
- It is defined as the capacity of the structure or the material to undergo large inelastic deformation without significant loss of strength or stiffness.

$$\text{Gauge length} = 5.65 \sqrt{A_0}$$

where,

A_0 = true sectional area of the specimen

$$\text{Percentage of elongation} = \frac{\text{elongated length} - \text{Gauge length}}{\text{Gauge length}} \times 100$$

Toughness

- It is defined as the capacity to absorb energy.
- It is a measure of the ability of steel to resist fracture under impact load.

Rolled Steel Section

1) I Section

2) Channel Section

3) Angle Section

4) T - Section

5) Tube Section

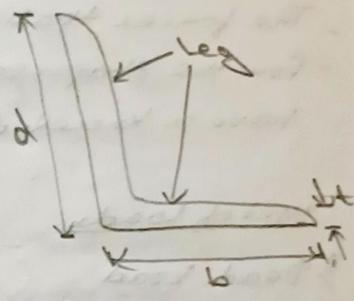
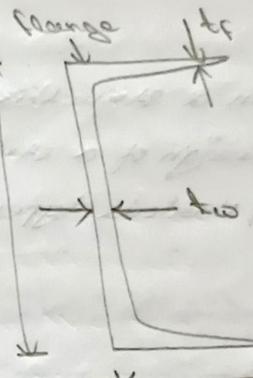
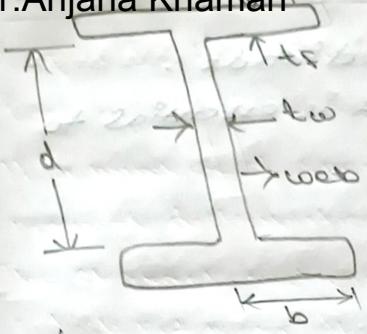
6) Flat Section

7) Plate Section

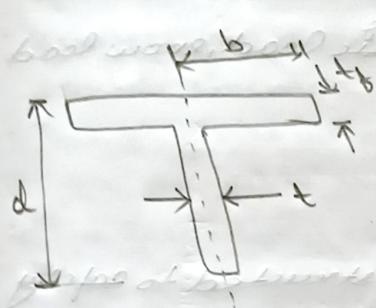
8) Sheet Section

9) Bar Section

10) Strip Section



(I-section) ~~is more strong than channel section~~
 is more strong (Channel section).



base plate

dimensions for select sheet

(T section), flange top frame is first all fitted
 dimensions will suggest, another of sheet, if dimension
 frame it will also

parallel to
 drawing paper will
 drawing will
 dimensions will be
 given with
 nothing will be
 associated with
 right
 corner will be

(flange) between parallel
 (flange) lower part will
 be marked first &

- The forces that act on a structure is called loads.
- For the safe design of a structure it is essential to have a knowledge of various types of loads.

Types of Loads

- 1) Dead Load
- 2) Live Load → earth pressure, water current load, impact load, Thermal load etc.
- 3) Environmental Loads → Wind load, Seismic load, snow load, rain load

Basic Design of Structure

Steel structure should be design and constructed to safely satisfy the design requirements for stability, strength, serviceability, brittle fracture, fatigue, fire and durability with due to economy.

Design Philosophy

- 1) Initial yielding
- 2) full yielding
- 3) Tensile strength
- 4) Critical buckling
- 5) Maximum deflection permitted
- 6) Stress concentration
- 7) Fatigue
- 8) Brittle fracture

- * Working stress method (elastic)
- * Limit design method (Plastic)
- * Limit state method

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- It is the elastic method of design.
- The lowest combination of working load is proportional to working stress.
- The factor of safety is defined as

$$FOS = \frac{\text{Working Stress}}{\text{Yield Stress}} = \frac{\text{Yield Stress}}{\text{Working Stress}}$$

- The analytical methods are based on assumptions and do not give the exact stresses.
- Structural members may temporarily be overloaded under certain circumstances.
- The stresses due to fabrication and erection are not considered in the design of ordinary structures.
- The secondary stresses may be appreciable.
- Underestimation of the future live load.
- Stress concentrations.
- Unpredictable material variations.

Plastic Method

- Steel is a ductile material and the stress-strain curve obeys the law over the structure up to yield stress.
- The plastic range means large strain.

Limit State Method

- It is similar to plastic design which considers most critical limit state and serviceability (design action < design strength).

Q) The yield strength for a mild strength specimen was found to 250 N/mm^2 . Taking a factor of safety of 2, find out the working stress.

Sol:-

Given data :-

For mild steel,

$$\text{Yield Strength} = 250 \text{ N/mm}^2$$

$$FOS = 2$$

$$\text{Working Stress} = \frac{\text{Yield Strength}}{FOS}$$

$$= \frac{250 \text{ N/mm}^2}{2}$$

$$= 125 \text{ N/mm}^2$$

Q) A tie bar $50 \text{ mm} \times 2 \text{ mm}^2$ is to carry a load of 20 kN . A specimen of the same quality steel of cross section area 250 mm^2 was tested in the laboratory. The maximum load carried by the specimen was 125 kN . Find the ultimate tensile strength factor of safety in the design and the gauge length.

Sol:-

Given data :-

Ultimate tensile strength for the steel

$$= \frac{\text{maximum load}}{\text{cross-sectional area}}$$

$$= \frac{125 \times 1000}{250}$$

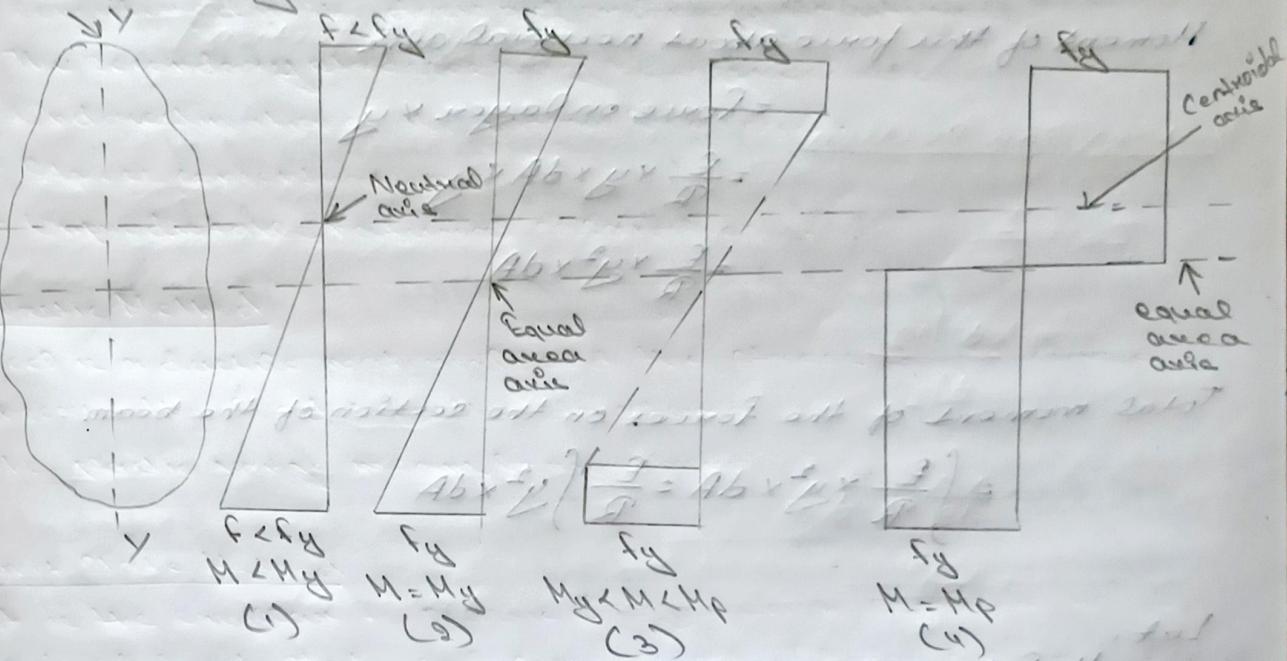
$$= 500 \text{ N/mm}^2$$

Plastic Analysis and Design

- Steel has unique physical property, ductility because of which it is able to absorb large deformation beyond the elastic limit without fracture.
- Plastic method of design uses
 - * Limit design
 - * Collapse method of design
 - * Ultimate design

Bending of BeamsArea $\frac{I}{J}$ - rigidity

Axis of symmetry



Development (in stages) of full plasticity of a beam section

Starting from zero moment, the beam will

$$M_p = \frac{\sigma_y I}{2} = \frac{f_y I}{2}$$

Moment of Resistance

Due to pure bending, the layers above the neutral axis are subjected to compressive stresses whereas the layers below the neutral axis are subjected to tensile stresses. Due to these stresses, the forces will be acting on the layers. These forces will have moment about the neutral axis. The total moment of these forces about the neutral axis for a section is known as moment of resistance of that section.

$$\text{Force on layer} = \frac{E}{R} \times y \times dA$$

Moment of the force about neutral axis

$$\begin{aligned} &= \text{Force on layer} \times y \\ &= \frac{E}{R} \times y \times dA \times y \\ &= \frac{E}{R} \times y^2 \times dA \end{aligned}$$

Total moment of the forces on the section of the beam.

$$= \int \frac{E}{R} \times y^2 \times dA = \frac{E}{R} \int y^2 \times dA$$

Let,

M = External moment applied on the beam section.

For equilibrium the moment of resistance offered by the section should be equal to the external bending moment.

$$\therefore M = \frac{E}{R} \int y^2 \times dA$$

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on $\int y^2 \times dA$ represents the moment of inertia of the area of the section about the neutral axis.

Let the moment of inertia be I .

$$\therefore M = \frac{F}{R} \times I \text{ or } \frac{M}{I} = \frac{F}{R}$$

From the equation (7.2), we have

$$\frac{\sigma}{y} = \frac{F}{R}$$

$$\frac{M}{I} = \frac{\sigma}{y} = \frac{F}{R} \quad (\text{Bending equation})$$

In this equation, the different quantities are expressed in consistent units as given:

M is expressed in Nm; I in mm^4

F is expressed in N/mm^2 ; y in mm

E is expressed in N/mm^2 ; R in mm

3/2/25

Shape factor (S)

It is defined as the ratio of the plastic moment and the yield moment of the section.

$$S = \frac{M_p}{M_y}$$

$$\Rightarrow S = \frac{\sigma_y Z_p}{\sigma_y Z_e}$$

$$\Rightarrow S = \frac{Z_p}{Z_e}$$

where,

Z_e = Elastic modulus

(Elastic modulus)

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$$Z_e = \frac{I}{Y}$$

where,

I = Moment of Inertia (Second moment of area)

Y = Distance of the extreme fibre distance from the neutral axis.

Z_p = Plastic modulus (It is the combine statistical moment of the cross sectional area above and below the equal area axis of a completely plastic yielding transverse stress at yield section)

Rectangular Section

$$Z_e = \frac{I}{Y}$$

$= \frac{bd^3/12}{d/2}$

$$= \frac{bd^3}{12} \times \frac{2}{d}$$

$= \frac{bd^2}{6}$

$$Z_p = \frac{bd^2}{Y}$$

$$S = \frac{Z_p}{Z_e}$$

$$= \frac{bd^2/4}{bd^2/6}$$

$$= \frac{bd^2}{12} \times \frac{4}{bd^2}$$

$$= 1.5$$

$$\frac{15}{10} = 1.5$$

$$\frac{15}{10} = 1.5$$

Factor of Safety (F)

It is defined as the ratio of the collapse load to the working load.

$$F = \frac{P_u}{P_w}$$

$$= \frac{M_u}{M_w}$$

$$= \frac{f_y Z_p}{f_{zc}}$$

$$\boxed{F = \frac{f_y}{f} \cdot S}$$

where,

$\frac{f_y}{f}$ = factor of safety

$$F.O.S = \frac{f_y}{f}$$

$$= \frac{f_y}{0.66 f_y} = 1.515$$

$$(\because f = 0.66 f_y)$$

↓
Permissible bending stress

Rectangular Section

$$F = 1.515 \times 1.5$$

$$= 2.2725$$

$$\approx 2$$

* for rectangular section:-

$$S = 1.5$$

$$f = 2$$

* for I section:-

$$S = 1.12$$

$$f = 1.7$$

Probabilistic basis for design for connection

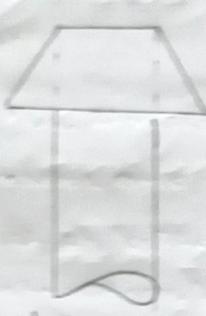
There are three types of connections:-

- 1) Riveted Connection
- 2) Bolted Connection
- 3) Pinned Connection

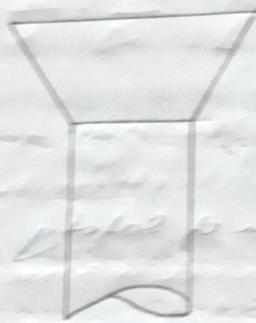
1) Riveted Connection



a) Snap



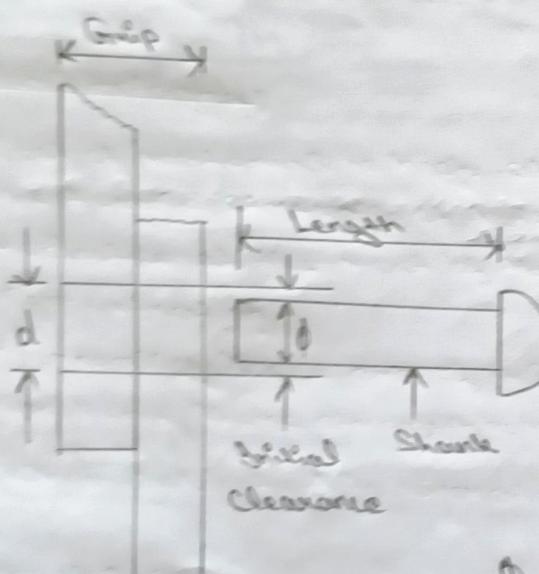
b) Pan



c) Flat
Countersink



d) Round
Countersink



Ø - Nominal diameter of rivet
d - True diameter of rivet

$E = ?$

- Probabilistic Basis

$P(A) = ?$

$E(A) = ?$

A rivet is made of a round ductile steel base piece (mild or high tensile) called shank, one with a head at one end.

Description

Shop rivets

Field rivets

Round head both sides



Countersunk nose side



Countersunk face sides



Countersunk both sides



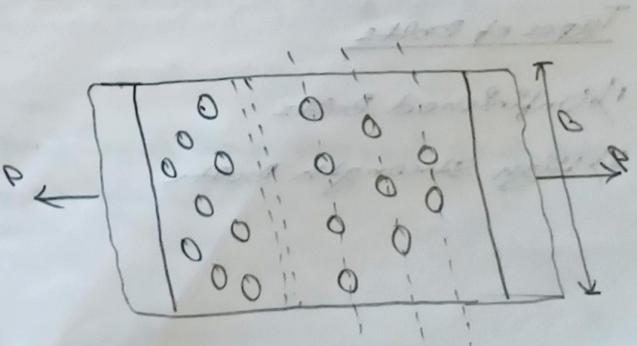
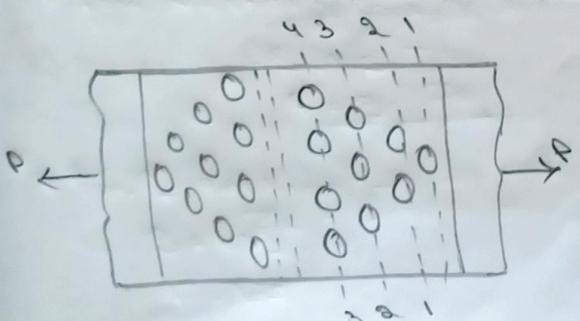
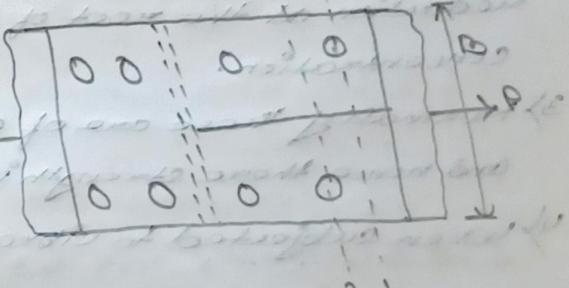
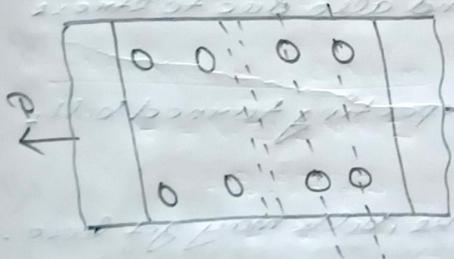
Patterns of Riveted Joints

1) Chain

2) Staggered chain

3) Diamond

4) Staggered diamond



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Welded Joint

- 1) The diameter of rivet to be used in the calculation is diameter of hole whereas for bolted connections it is the nominal diameter of bolt in case the holes are drilled.
- 2) The design stresses are slightly different lesser for bolts.

Bolted Connections

The bolt may be defined as a metal pin with a head at one end and a shank threaded at the other end to receive a nut.

Advantages

- 1) The erection of the structure can be speeded up.
- 2) Less skilled persons are required.
- 3) The overall cost of bolted construction is cheaper than that of riveted construction because of reduced labour and equipment costs and the smaller number of bolts required resisting the same load.

Disadvantages

- 1) Cost of material is high, about double that of rivets.
- 2) The tensile strength of bolt is reduced because of area reduction at the root of the thread and also due to stress concentration.
- 3) Normally there are of a loose fit respecting turned bolts and hence their strength is reduced.
- 4) When subjected to vibrations or shocks, bolts may get loose.

Types of Bolts

- 1) Unfinished Bolts
- 2) High Strength Bolts

1) Unfinished Bolts

Unfinished bolts are called ordinary, common rough or black bolts. These are used for light structures subjected to static loads and for secondary members such as girders, bearings, roof trusses etc.

2) High Strength Bolts

The high strength bolts are made from bars of medium carbon heat treated steel and from alloy steel.

Advantages

- HSFH bolts provide a rigid joint. There is no slip between the elements connected.
- Large tensile stresses are developed in bolts, which in turn provide large clamping force to the element connected.
- There is no stress concentration in holes, and therefore the fatigue strength is more.
- Few persons are required to make the connections, thus cost is reduced.
- Noise nuisance is not there and there is no danger of tearing of the rivet.
- Alterations can be done easily.

Types of Bolted Joints

- 1) Lap Joint
- 2) Butt Joint

1) Lap Joint

The two members to be connected are overlapped and connected together. Such a joint is called lap joint.

2) Butt Joint

The two members to be connected are placed end to end. Such a joint is called butt joint.

Friction Transfer Mechanism

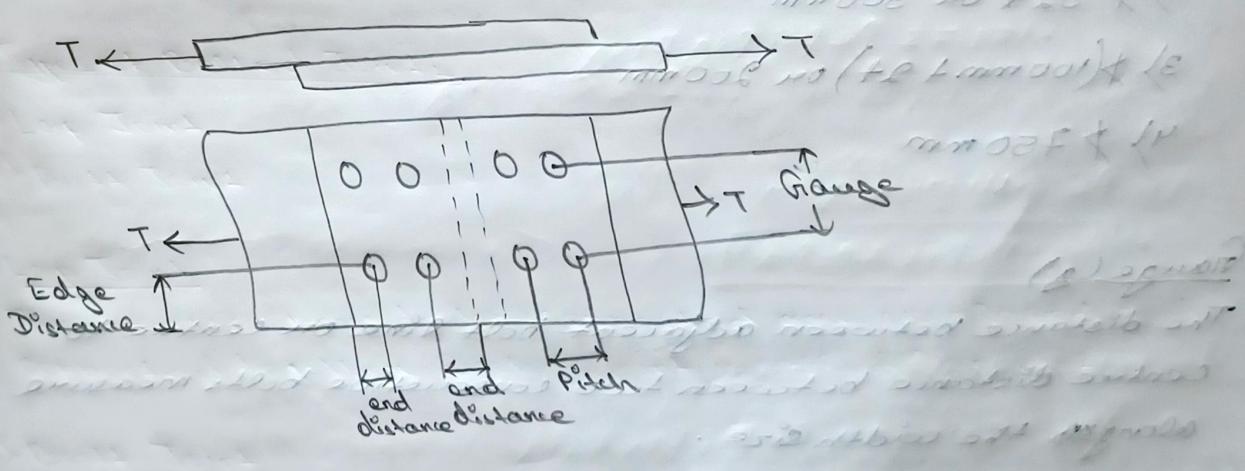
- Depending upon the type of bolts - ordinary or high strength bolts - the load transfer from one connected part to another may be by shear and bearing or by friction.
- The former being called bearing type connection and the latter the slip - critical or slip - resistant connection.
- The connection made with high - strength bolts may, however be slip - resistant or bearing type.

Failure of Bolted Joint

- 1) Shear failure of bolts
- 2) Bearing failure of bolts
- 3) Tension failure of bolts
- 4) Tension or tearing failure of bolts
- 5) Block shear failure

Shear failure of bolts

Specification for bolted joints



(Double cover butt joint)

Diameter of Bolt

The large diameter of bolt are favourable in connection where shear governs because, the bolt capacity in shear is proportional to square of the bolt diameter.

Spacing of Bolt hole

* Pitch (P)

It is the distance between the centre of two consecutive bolts measured along a row of the column.

* Minimum Pitch

To prevent bearing failures of members between the two bolts. Less than 2.5 times of the nominal diameter of the bolt.

* Maximum Pitch

To reduce the length of the connection and gasket plate.

Limit of Pitch

1) $\geq 16t$ or 200 mm (Tension members)

2) $\geq 12t$ or 200 mm (Compression members)

3) $\geq 32t$ or 300 mm

4) $\geq (100\text{mm} + 2t)$ or 200 mm

5) ≥ 750 mm

Gauge (g)

The distance between adjacent bolt line on centre to centre distance between two consecutive bolts measured along the width size.

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1) Shearing strength of bolt

2) Bearing strength of bolt

3) Tensile strength of bolt

1) Shearing strength of bolt

The nominal shear capacity of bolt

$$V_{nab} = \frac{f_{ub}}{\sqrt{3}} (n_{ab} A_{sh} + n_{afe} A_{sh})$$

The nominal shear capacity of bolt for long joint will be less i.e.

$$V_{nab} = \frac{f_{ub}}{\sqrt{3}} (n_{ab} A_{sh} + n_{afe} A_{sh}) \beta_{ej} \beta_{lg} \beta_{pg}$$

where,

V_{nab} = Nominal shear capacity of the bolt

f_{ub} = Ultimate tensile stress of the bolt

n_{ab} = Number of shear planes with threaded intercepting the shear plane.

n_{afe} = Number of shear plane without threaded intercepting the shear plane

A_{sh} = Net tensile stress area

A_{sh} = Nominal shank area

n = Number of shear plane

β_{ej} = A reduction factor to allow for the overloading of the end ^{bolt} that occurs in longer connection.

β_{lg} = A reduction factor to allow for the effect of the large gage length.

β_{pg} = A reduction factor to account for galling plate in excess of 26 mm

Bolt diameter (mm)	12	16	20	22	24	27	30	36
Amb (mm²)	84.3	157	245	303	353	459	561	817

8/2/25

For the safety of joints in shear, the strength of bolt Web
and flange plate

$$V_{eb} \leq \frac{V_{nrb}}{\gamma_{mb}}$$

Where,

$$(n_f A_f + n_b A_b) \frac{d_u}{E_l} = v_{eb}$$

γ_{mb} = Partial safety factor for the material of bolt

two part of the flange plate column

$$V_{eb} = \frac{V_{nrb}}{\gamma_{mb}}$$

$$= \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \times (n_f A_f + n_b A_b) \beta_{ej} \beta_{eg} \beta_{pg}$$

For 4.6 grade steel bolt,

$$f_{ub} = 400 \text{ MPa}$$

$$V_{eb} = \frac{400}{\sqrt{3} \times 1.25} \times (n_f A_f + n_b A_b) \beta_{ej} \beta_{eg} \beta_{pg}$$

$$= 184.75 \text{ N ej eg pg kg}$$

Where,

A_e = effective area

$$\Rightarrow A_e = n_f A_f + n_b A_b$$

For bolt in double shear, v_{eb} = 2×184.75 N ej eg pg kg

$$V_{eb} = 2 \times 184.75 A_e \beta_{ej} \beta_{eg} \beta_{pg}$$

good frag - good not

group of two most tensile members $A = 607$
and $E_l = 200 \text{ GPa}$

Reduction factor for Long Joint (β_{pj})

Er. Anjana Khamari

- When the length of the joint exceeds 15d in the direction of the load the shear capacity of the joint is reduced.

$$\beta_{pj} = 1.075 - \frac{lg}{200d} \quad (\text{for } 0.75 \leq \beta_{pj} \leq 1.0)$$

Where,

lg = length of the joint (The diameter between the 1st and last row of bolt in a joint measure in the direction of load transfer)

* The reduction factor = 1

Reduction factor for Large grip length (β_{lg})

- When the grip length of the bolt increases, the bolt is subjected to a greater bending moment due to shear force acting on its shank.

$$\beta_{lg} = \frac{ld}{3d + lg}$$

Where,

lg = grip length

Reduction factor for packing plates (β_{pkg})

- When the packing plates are more than 6mm in thickness, the shank of the bolt bolt is subjected to bending which affects the nominal shear capacity of the bolt.

$$\beta_{pkg} = (1 - 0.0125 t_{pkg})$$

Where,

t_{pkg} = thickness of the thinner packing plate in mm

Nominal bearing strength of bolt

$$V_{pb} = 2.5 k_b d t f_u$$

Where,

$$k_b = \text{smaller of } \left\{ \begin{array}{l} \frac{e}{3d_0} \\ \frac{t}{3d_0} - 0.25 \\ \frac{f_{ub}}{f_u} \\ 1.0 \end{array} \right\}$$

Where,

d_0 = diameter of hole

e = end and point distance of the fastener along bearing direction.

f_{ub} = ultimate stress of bolt

f_u = ultimate tensile stress of the plate in MPa

d = Nominal diameter of the bolt in mm

t = aggregate thickness

for the safety of the joint in bearing,

$$V_{pb} \leq \frac{V_{pb}}{\gamma_{mb}}$$

Where,

γ_{mb} = the specified safety factor for material of bolt
= 1.25

$\therefore V_{pb} = 2.5 k_b d t f_u$

$$V_{pb} = 2.5 k_b d t \frac{f_u}{\gamma_{mb}}$$

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The nominal capacity of bolt,

$$T_{nb} = 0.9 f_{ub} A_{nb}$$

$$\angle f_{yb} A_{sb} \frac{Y_{mb}}{Y_{mo}}$$

Where,

f_{ub} = ultimate tensile stress of bolt

f_{yb} = yield stress of bolt

A_{nb} = net tensile stress area of bolt

A_{sb} = shank area of bolt

The bolt is safe in tension if the factored tension force,

$$T_{db} \leq \frac{T_{nb}}{Y_{mb}}$$

Where,

Y_{mb} = the partial safety factor for material of bolt
= 1.25

Y_{mo} = Partial safety factor for material resistance governed
by yielding = 1.10

$$T_{db} = 0.9 \frac{f_{ub}}{Y_{mb}} A_{nb}$$

Tensile Strength of Plate

Net area $A_n = (B - n d_n) t$, for chain bolting

for staggered bolting,

$$A_n = \left[B - n d_n + \sum_{i=1}^m \frac{P_{bi}^2}{4 g_i} \right] t$$

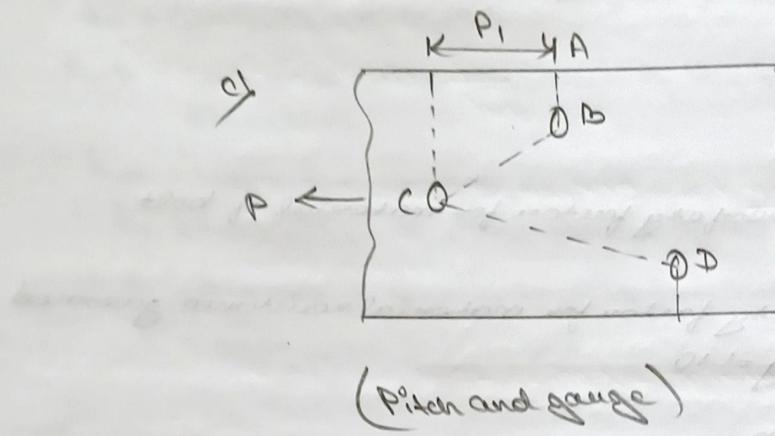
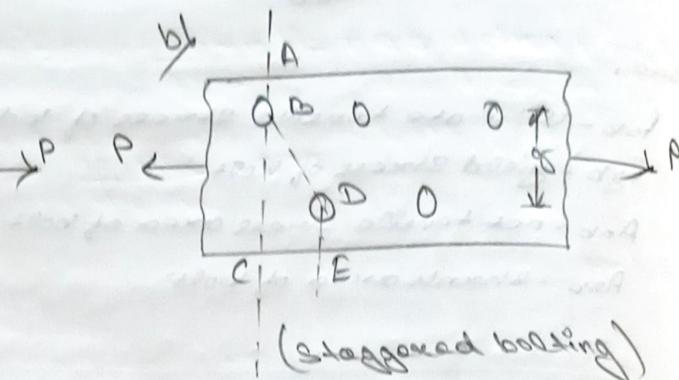
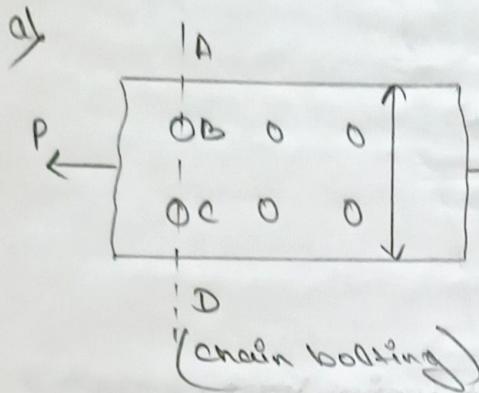
The tensile strength of the plate is given by

$$T_{nd} = 0.9 A_n \frac{f_u}{Y_{ml}}$$

f_u = the ultimate stress of material in MPa

A_n = the net effective area in mm²

γ_{ML} = partial safety factor = 1.25



Strength and Efficiency of the Joint

Efficiency of a bolted joint, (η)

(η) is also called the percentage strength of the joint

$$\eta = \frac{\text{Strength of bolted joint / Pitch length}}{\text{Strength of solid plate / Pitch length}} \times 100$$

Q) Calculate the strength of a 20 mm diameter bolt of grade 4.6 for the following cases. The main plates to be jointed are 12 mm thick.

a) Lap Joint

b) Single cover butt joint, the cover plate being 10 mm thick.

c) Double cover butt joint; each of the cover plate being 8 mm thick.

Soln

Given data :-

for grade 4.6,

$$f_{ub} = 400 \text{ MPa (for bolt)}$$

for Fe 410 grade of steel,

$$f_u = 410 \text{ MPa (for steel)}$$

$$V_{mb} = 1.25 \text{ (permitted safety factor for bolt)}$$

Diameter of bolt, $d = 20 \text{ mm}$

$$A_{nb} = 245 \text{ mm}^2$$

a) For Lap joint :-

Strength of bolt for single shear,

$$V_{eb} = A_{nb} \frac{f_{ub}}{\sqrt{3} V_{mb}}$$

$$= 245 \text{ mm}^2 \times \frac{400 \text{ MPa}}{\sqrt{3} \times 1.25} \times 10^{-3}$$

$$= 45.26 \text{ kN}$$

From table 24.3

$$d = 20 \text{ mm}$$

$$d_o = 22 \text{ mm}$$

$$e = 23 \text{ mm}$$

Assume,

$$P = 50 \text{ mm}$$

Er. Anjana Khamari

$$V_{pb} = 2.5 \text{ kN} \cdot t \frac{f_u}{Y_{mb}}$$

$$\left. \begin{aligned} k_b &= \text{less of } \left\{ \begin{aligned} \frac{\ell}{3d_o} &= \frac{33 \text{ mm}}{3 \times 22 \text{ mm}} = 0.5 \\ \frac{\ell}{3d_o} - 0.25 &= \frac{50 \text{ mm}}{3 \times 22 \text{ mm}} - 0.25 = 0.51 \\ \frac{f_{ub}}{f_u} &= \frac{400 \text{ MPa}}{410 \text{ MPa}} = 0.98 \end{aligned} \right. \end{aligned} \right\}$$

$$\text{So, } k_b = 0.5$$

$$V_{pb} = 2.5 \text{ kN} \cdot t \frac{f_u}{Y_{mb}}$$

$$= 2.5 \times 0.5 \times 20 \text{ mm} \times 12 \text{ mm} \times \frac{40 \text{ MPa}}{1.25} \times 10^{-3}$$
$$= 28.4 \text{ kN}$$

∴ The strength of the bolt will be minimum in shear and bearing
i.e. 45.26.

b) For single cover bolt joint $t = 10 \text{ mm}$

$$\text{The strength of bolt in single shear} = 45.26 \text{ kN}$$

The strength of bearing,

$$V_{pb} = 2.5 \text{ kN} \cdot t \frac{f_u}{Y_{mb}}$$

$$= 2.5 \times 0.5 \times 20 \text{ mm} \times 10 \text{ mm} \times \frac{410 \text{ MPa}}{1.25} \times 10^{-3}$$
$$= 82 \text{ kN}$$

So, strength of the bolt is 45.26 kN.

The strength of bolt in double shear,

$$V_{bs} = 2 \times A_{ns} \frac{f_y}{\sqrt{3} V_m b}$$

$$= 2 \times 245 \times \frac{400}{\sqrt{3} \times 1.25} \times 10^3$$

$$= 90.52 \text{ kN}$$

The strength of bolt in bearing,

$$V_{pb} = 2.5 K_b d t \frac{f_y}{V_m b}$$

$$= 2.5 \times 0.5 \times 20 \times 12 \times \frac{410}{1.25} \times 10^3$$

$$= 98.4 \text{ kN}$$

The strength of the bolt will be minimum of the strength in shear and bearing i.e. 90.25 kN.

Minimum Edge Distance of bolts

Nominal diameter of bolt (mm) (d)	Diameter of hole (mm) (d ₀ or d ₁)	Distance of sheared on hand flame cut edge (mm)	Distance to machine flame cut, sever or planed edge, (e) (mm)
12	13 and above	20	19
14	15	26	23
16	18	30	27
18	20	34	30
20	22	37	33
22	24	40	36
24	26	44	39
27	30	51	45
30	33	56	50
Over 33 mm	Bolt diameter + 3 mm	1.7 x hole diameter	1.5 x hole diameter

If a single-bolted double-cover butt joint is used to connect two plates which are 8 mm thick. Assuming 16 mm diameter bolts of grade 4.6 and cover plates to be 6 mm thick, calculate the strength and efficiency of the joint if 4 bolts are provided in the bolt line at a pitch of 45 mm.

Also determine the efficiency of the joint if two lines of bolts with two bolts in each line have been arranged to result in a double-bolted double-cover butt joint.

Soln

Given data →

For Fe 410 grade of steel,

$$f_u = 410 \text{ MPa}$$

For bolts of grade 4.6,

$$f_{ub} = 400 \text{ MPa}$$

For 16 mm dia bolt,

$$A_{nb} = 157 \text{ mm}^2$$

$$\gamma_{mb} = 1.25$$

$$\gamma_{ml} = 1.25$$

$$t = 8 \text{ mm}$$

$$\text{Plate thickness } (t) = 8 \text{ mm}$$

$$\text{Cover plate thickness } (t_c) = 6 \text{ mm}$$

$$\text{Bolt diameter } (d) = 16 \text{ mm}$$

$$\text{Bolt grade} = 4.6$$

From Table 4.3 →

For 16 mm dia bolt,

$$A_{nb} = 157 \text{ mm}^2$$

$$\gamma_{mb} = 1.25$$

$$\gamma_{ml} = 1.25$$

$$V_{pb} = 2 \times A_{nb} \times \frac{f_u}{\sqrt{3} V_{mb}}$$

$$= 2 \times 157 \times \frac{400}{\sqrt{3} \times 1.25} \times 10^{-3}$$

$$= 58 \text{ kN}$$

$$t = 2 \text{ mm}$$

The strength of bolt in bearing per pitch length,

$$\Rightarrow V_{pb} = 2.5 \text{ kN} \times \frac{f_u}{V_{mb}}$$

$$k_b = \text{least of } \left\{ \begin{array}{l} \frac{\ell}{3d_0} = \frac{3}{3 \times 18} = 0.55 \\ \frac{\ell}{3d_0} - 0.25 = \frac{45}{3 \times 18} - 0.25 = 0.52 \\ \frac{d_{ub}}{d_u} = \frac{400}{410} = 0.975 \end{array} \right.$$

$$k_b = 0.55$$

$$V_{pb} = 2.5 \times 0.55 \times 16 \times 8 \times \frac{400}{1.25} \times 10^{-3}$$

$$= 56.31 \text{ kN}$$

The net strength of plate per pitch length,

$$T_{nd} = 0.9 \frac{f_u}{V_{mb}} A_n$$

$$T_{dn} = 0.9 \frac{f_u}{V_{mb}} (P - d_t) t$$

From table 4.2,

$$T_{dn} = 0.9 \times \frac{410}{1.25} (45 - 18) \times 8 \times 10^{-3}$$

$$= 63.76 \text{ kN}$$

Strength of the solid plate per pitch length,

$$= 0.9 \frac{f_u}{V_{mb}} P t$$

$$= 0.9 \times \frac{410}{1.25} \times 45 \times 8 \times 10^{-3}$$

$$= 106.97 \text{ kN}$$

the strength of the joint per pitch length = 66.31 kN

$$\text{Efficiency of the joint} = \frac{66.31}{106.27} \times 100 \\ = 62.22\%$$

When the bolts are arranged in the rows the strength of the joint per pitch length on the basis of

a) Shear = $2 \times 58 = 116$ kN

b) Bearing = 2×56.31
= 112.62 kN

c) Net tensile strength = 63.76 kN

So strength of the joint per pitch length = 63.76 kN

$$\text{Efficiency of the joint} = \frac{63.76}{106.27} \\ = 59.99\%$$

18/9/25

Simple welded Connection (chapter)

Introduction

- When two structural members are joined by means of welds, the connection is called a welded connection.
- Welded design offer the opportunity to achieve a more efficient use of materials.
- The speed of fabrication and execution helps compressed production schedules.
- Welding saves weight and consequently cuts costs.
- No deductions are there for holes, thus the gross section is effective in carrying loads.
- Welded joints are better for fatigue loads, impact loads and vibrations.

Types

- 1) Fillet weld
- 2) Groove weld
- 3) Plug weld
- 4) Slot weld
- 5) Spot weld

Assumptions of welded joint

- Er. Anjana Khamari
- The welding connection various parts are homogeneous, inelastic and elastic elements.
 - The part connected by the weld are rigid and their force of deformation are neglected.
 - Only stress due to external loads are considered.

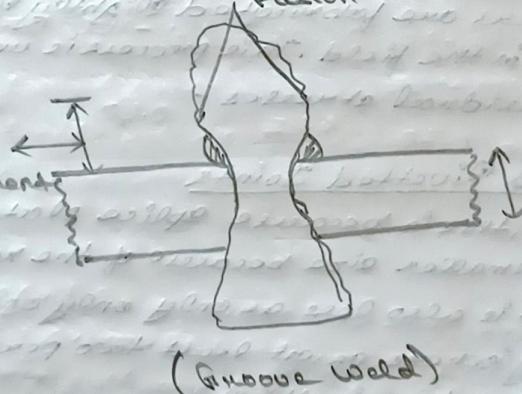
Design of groove welds

- Groove and filleted weld are most frequently used.
- Groove welds are provided when the members to be joined are lined up.
- It requires edge preparation are costly.

Type of groove weld

- 1) Square
- 2) Single VEE
- 3) Double VEE
- 4) Single V
- 5) Double V
- 6) Single Tee
- 7) Double Tee
- 8) Single be Ve
- 9) Double be Ve

Fusion zone



Design Strength

- The strength of the groove weld in tension or compression is governed by yield.

$$T_{dw} = \frac{f_y L_w t_e}{\sqrt{m_w}}$$

where,

f_y = smaller of yield stress of the weld (f_{yw}) and the parent metal (f_y) in MPa.

L_w = effective length of the weld in mm

t_e = effective throat thickness of the weld in mm.

Your partial safety factor
 $= 1.25$ for shop welding
 $= 1.5$ for site welding

- The design strength of the butt weld in shear is also governed by yield.

$$V_{dw} = \frac{f_{yw} L_w t_e}{\gamma_{mw}}$$

Where,

f_{yw} = smaller of shear stress of weld ($f_y w / \sqrt{3}$) and the parent metal ($f_y / \sqrt{3}$)

γ_{mw} = Partial safety factor as defined above.

f_{yw} = yield stress of weld (Mpa)

Design of fillet welds :-

- The fillet weld is done for members which overlap each other. For such joints the critical stress is shear stress.

Fillet weld Vs Butt weld

- 1) A fillet weld saves the operations of Veeing and finishing the ends of members.
- 2) In case of butt weld, members are fabricated slightly long and cut exactly to have a close fit in the field. This process is uneconomical.
- 3) Butt welds have higher residual stresses.

Welded joints Vs Bolted and Riveted Joints

- 1) Welded joints are economical, this is because splice plates and bolts riveted materials are of a smaller size because of the reduced connection length. Labour cost is also less as only one person is required to do the welding whereas at least two persons are required for bolting and four for rivetting.
- 2) Welded structures are more rigid as compared to bolted/riveted joints. In bolted/riveted joints, cover plates, connecting angles etc. deflect along with the member during load transfer and make the joint more flexible.
- 3) Due to the fact that the strength of a welded joint is the same as that of the parent metals, even a smallest piece of the metal which otherwise is a scrap can be used, bringing overall economy.
- 4) With welding it has become possible to connect tubular sections, which are structurally very economical.

Due to the fusion of two metal pieces jointed, a continuous structure which gives a better architectural appearance than bolted/riveted joints.

Advantages can be done with less expense in case of welding as compared to bolting/riveting.

The process of welding is quicker in comparison to bolting/riveting.
The process of welding is silent, whereas in the case of riveting a lot of noise produced.

In welding less safety precautions are required for the public in the vicinity, whereas a hot rivet may fall and injure the person working.

As slice plates, bolts/rivets are not used, the details and drawings of welded structures are easier and less time consuming.

20/9/25

and joint assembly

(ad) tributary base area (ad) net

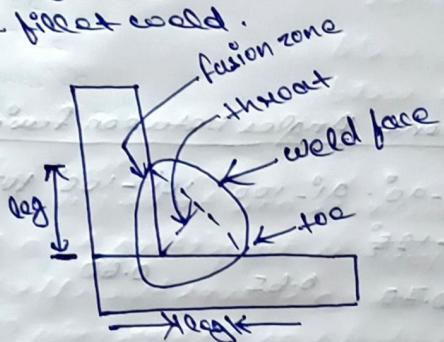
Design of Fillet Welds

Size(s) :-

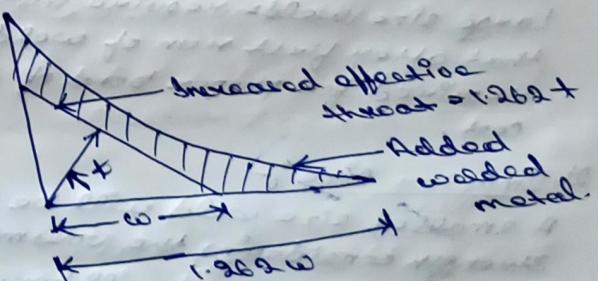
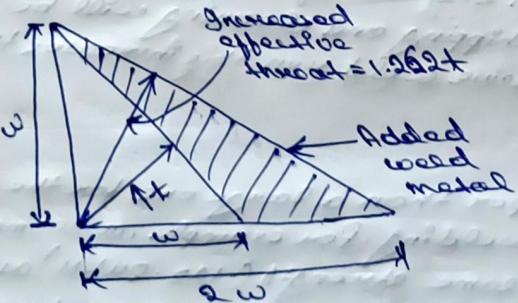
The minimum leg length of the weld.

Leg length :-

The leg length is the distance from the root to the toe of the weld of the fillet weld.



- It is measured by the longest right angle triangle which can be inscribed within the weld.



Size of weld① Maximum size of weld

It is obtained by subtracting 1.5mm from the thickness of the thinner member to be jointed.

② Minimum size of weld

The weld size should not be less than 3 mm

Table 5.4Minimum size of weldThickness of thinner memberMinimum size (mm)

<u>Over (mm)</u>	<u>Upto and including (mm)</u>
0	10
10	20
20	32
32	50

Table 5.5Values of constant K for Different Angles between fusion faces

Angle between fusion faces	$60^\circ - 90^\circ$	$90^\circ - 100^\circ$	$100^\circ - 105^\circ$	$105^\circ - 110^\circ$	$110^\circ - 115^\circ$	$115^\circ - 120^\circ$
K	0.70	0.70	0.65	0.60	0.55	0.50

No. of minimum size1) Large size %

Large size welds require more than one run of welding which means that after first run of welding chipping and cleaning will be required for proper bond of successive weld runs this increases the cost.

2) Small size %

A smaller size weld will be cheaper than a large one for the same strength considering the volume of welding. For example, a 300mm, 5mm size fillet weld will have the same strength (198.24 kN) as a 150 mm long and 10 mm size fillet weld. However the volume of weld metal for a 10 mm weld will be $\left[\frac{1}{2} \times 10^2 \times 150 = 7500 \text{ mm}^3\right]$

which is about twice that of 5mm size weld,

$$\left[\frac{1}{2} \times 5^2 \times 300 = 3750 \text{ mm}^3\right]$$

Effective throat thickness

EN Anjana Khamari
The shoulder distance from the root of the fillet weld to the face of the diagrammatic weld (line joining to the c)

- Effective throat thickness should not be less than 3mm.
- It should not exceed 0.7t or 1.0t

where,

t = thickness of thinner plate of elements being welded.

Effective throat thickness

$$= k \times \text{size of weld}$$

$$= k \times l$$

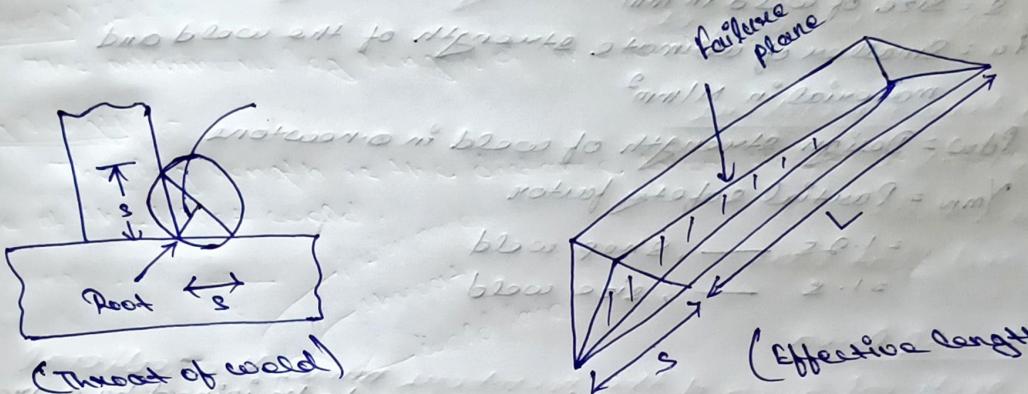
where,

$$l = \text{size of weld in mm}$$

$k = \text{constant}$

$$\text{Throat} = kl$$

$$= 0.7075$$



* Fillet weld is not recommended if the angle between tension force is less than 60° or more than 120° . For long joints the design capacity of weld is reduced by a factor.

$$\beta = 1.2 - \frac{0.2 l_j}{150} \leq 0.1$$

where,

l_j = length of joint in the direction of force transfer.

t_w = throat size of the weld

Effective Area

It is equal to effective length of weld multiplied by effective throat thickness.

Design Strength

Design strength of a fillet weld,

$$f_w = \frac{f_w n}{\sqrt{m_w}}$$

Non-nominal nominal strength of fillet weld

$$= \frac{f_u}{\gamma_m}$$

The design strength of a fillet weld is based on the given by,

$$P_{dw} = f_u \frac{l_e}{\gamma_m \gamma_w}$$

or,

$$= L_w t_e \frac{f_u}{\gamma_m \gamma_w}$$

where,

L_w = effective length of weld in mm

t_e = throat thickness in mm

t = size of weld in mm

f_u = Smaller of ultimate strength of the weld and material in N/mm²

P_{dw} = Design strength of weld in connection

γ_m = Partial safety factor

= 1.25 — shop weld

= 1.5 — size weld

4/3/25

Bx-5.1

Two plates of 16 mm and 14 mm thickness are to be joined by a groove weld as shown in fig. Bx-5.1. The joint is subjected to a factored tensile force of 430 kN. Due to some reasons the effective length of the weld that could be provided was 175 mm only. Check the safety of the joint if

a) single V groove weld is provided.

b) double V groove weld is provided.

Assume the plates to be shop welded ($\gamma_m = 1.25$)

Sol:

Given :-

a) Single V groove weld :-

Tensile force = 430 kN

for Fe 410 grade of steel,

$$f_u = 350 \text{ N/mm}^2$$

$$= \frac{S}{2} \times 14 \text{ mm}$$

$$= 8.75 \text{ mm}$$

For shop weld,

$$\gamma_{mw} = 1.25$$

Effective length of weld,

$$L_w = 175 \text{ mm}$$

Strength of the weld,

$$T_{dw} = L_w t_e \frac{\gamma}{\gamma_{mw}}$$

$$= 175 \times 8.15 \times \frac{250 \text{ MPa}}{1.25}$$

$$= 175 \times 8.15 \times \frac{250 \times 10^6 \text{ N/mm}^2}{1.25}$$

$$= 306.25 \text{ kN} < 430 \text{ kN thickness (t)}$$

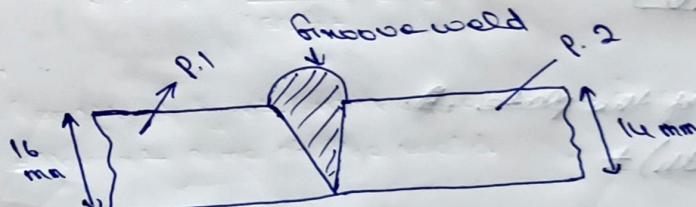
sook (not ok)

b) Double-V groove weld °-

$$T_{dw} = L_w t_e \frac{\gamma}{\gamma_{mw}}$$

$$= 175 \times 14 \times \frac{250 \times 10^6 \text{ N/mm}^2}{1.25}$$

$$= 490 \text{ kN} > 430 \text{ (OK)}$$



TENSION MEMBERIntroduction

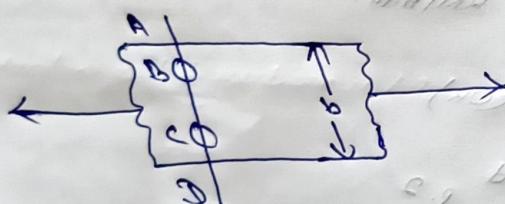
- A structural member subjected to two pulling tensile forces applied at its ends is called a tension member.
- The stress in an axial load, tension member can be determined by axial load with its cross-sectional area.
- e.g.
- e.g.
- 1) Tension in building and bridge
- 2) Communication and satellite to use
- 3) Tie in lattice girder
- 4) Bracing system in multistory building
- 5) Industrial building etc

Types of tension members

- 1) Chain and cable
- 2) Bar and node
- 3) Plates and flat base

Net sectional Area

- It is the sectional area of the member, minus the sectional area of the maximum number of holes.



Net sectional area of the plate, A_n

$$A_n = (b - ndn)t$$

Where,

b = width of the plate

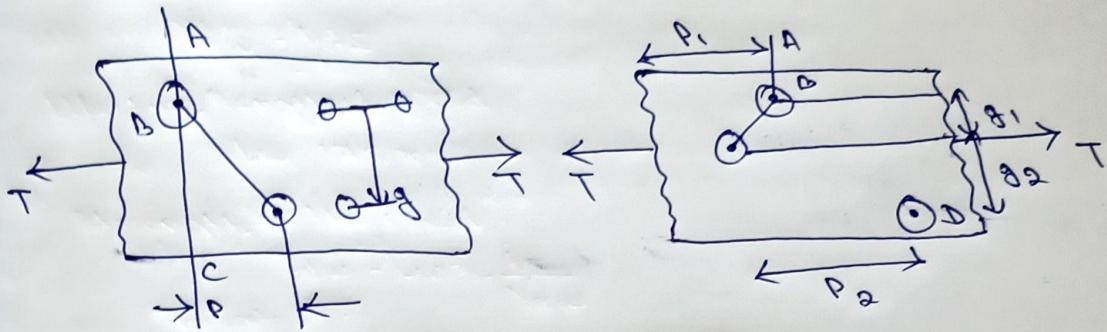
n = no. of bolts

d_n = dia of the bolt hole

t = thickness of plate

$$A_n = A_g$$

where,

 A_g = gross-cross sectional area of the plate

$$A_n = A_g - \left[\text{sectional area of the hole} \right] = \left(\frac{\rho_1^2 t}{4g_1} + \frac{\rho_2^2 t}{4g_2} \right)$$

$$= bt - \left[ndht - \left(\frac{\rho_1^2 t}{4g_1} + \frac{\rho_2^2 t}{4g_2} \right) \right]$$

$$= bt - ndht + \frac{\rho_1^2 t}{4g_1} + \frac{\rho_2^2 t}{4g_2}$$

$$= \left(b - ndht \right) \frac{\rho_1^2}{4g_1} + \frac{\rho_2^2}{4g_2} t$$

$$\text{If, } \rho_1 = \rho_2 = \rho$$

$$g_1 = g_2 = g$$

then,

$$A_n = \left(b - ndht + \frac{\rho^2}{4g} + \frac{\rho^2}{4g} \right) t$$

$$= \left(b - ndht + \frac{2\rho^2}{24g} \right) t$$

$$\Rightarrow A_n = \left(b - ndht + \frac{\rho^2}{2g} \right) t$$

where,

 ρ = Pitch distance g = Gauge distance